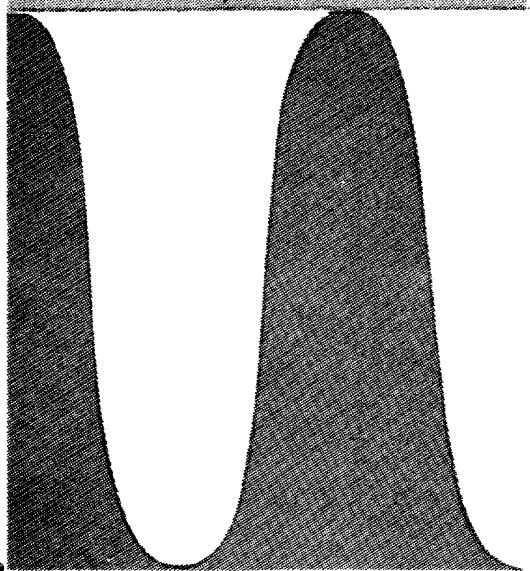


THE UNIVERSITY
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madison, wisconsin



A PROGRAM FOR THE SOLUTION OF DIFFERENTIAL
EQUATIONS USING INTERVAL ARITHMETIC
(DIFEQ)

For the CDC 3600 and 1604

J. A. Braun and R. E. Moore

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MRC Technical Summary Report #901
June 1968

UNITED STATES ARMY

MATHEMATICS RESEARCH CENTER



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ABSTRACT

A practical implementation of the techniques of interval analysis developed by Professor R. E. Moore (Interval Analysis, Prentice-Hall, 1966) is described for solving systems of differential equations on the CDC 3600 and 1604.

A PROGRAM FOR THE SOLUTION OF DIFFERENTIAL
EQUATIONS USING INTERVAL ARITHMETIC
(DIFEQ)

For the CDC 3600 and 1604

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Purpose

To provide a numerical solution, together with machine computed error bounds, for systems of N first order differential equations. Error bounding is rigorous, completely automatic and includes truncation errors, round-off errors and errors in initial data. This package is designed for use with FORTRAN. For a full description of the theory behind DIFEQ, see [1]

Input

The first two data cards contain respectively, in I3 format, the size, N , of the system and the number of terms NDER, to be taken in the Taylor expansion. The next three data cards contain respectively, in E20.8 format, the starting value TSTART, of the independent variable, the final value, TFINAL, of the independent variable and the printing interval DELTAT of the independent variable. The next set of data cards contains the system of equations, subject to the rules contained in Formulae below. The final data cards contain, in C(E20.8, E20.8) format, the initial conditions, given as intervals — degenerate or otherwise — and appearing in the order y_1, y_2, y_3 , etc.

See EXAMPLES below for illustrations.

Program DIFEQ is written for use with FORTRAN 63 on the CDC 3600 and 1604.

Sponsored by the Mathematics Research Center, United States Army, Madison, Wisconsin, under Contract No.: DA-31-124-ARO-D-462.

Formulae

The system of equations is to be given in strings of first order equations, all equations ending with a terminating character "\$" . One must supply N^{\dagger} equations defining the dependent variables. A dependent variable name is a string of two or three alphanumeric characters, the first of which must be a Y . The name of the derivative of the dependent variable is like the dependent variable with the exception that the first character must be a D . In the equations all variable names, operator names, left parentheses, right parentheses, termination characters (i.e. \$) and equality signs must be separated from each other by at least one blank, (subsequent blanks will be ignored) and contain no blanks within themselves. As usual, columns 73-80 will be ignored.

If a parameter is to be used its name must be any string of one, two or three letters the first of which must be an M, (e.g. MU). A shorthand variable may be used and its name may be any string of one, two, or three letters, the first of which is not a Y, D, or M . All constants may appear signed or unsigned in Integer, E or F format. All of these cards will be read in until N dependent variables have been read in. The equations may be strung out over many cards, or several formulas may appear on one card. The termination character signifies the end of one equation and the end of a card has no real significance.

EXAMPLES

1.) PROBLEM: $\frac{dy}{dx} = 2y, \quad y(0) = 1$

INPUT DATA DECK: 001
010
0.0
0.1
D1 = 2 * Y1 \$
1.0

[†] N equals the size of the system.

These cards correspond respectively to:

N, Size of system;

NDER, Number of Taylor series terms to be used;

TSTART, Initial value of x ;

TFINAL, Final value of x ;

DELTAT, Print interval;

The Differential Equation ;

Initial value of y .

2.)

PROBLEM: $\frac{dy}{dx} = y^2 \quad y(0) = 1$

INPUT DATA DECK: 001
 010
 0.0
 1.0
 0.1
 D1 = Y1 ** 2 \$
 1.0

3.)

PROBLEM: $\ddot{x}_1 - 2\dot{x}_2 = x_1 - \frac{\mu(x_1 - 1 + \mu)}{r^3} - \frac{(1 - \mu)(x_1 + \mu)}{R^3}$

$$\ddot{x}_2 + 2\dot{x}_1 = x_2 - \frac{\mu x_2}{r^3} - \frac{(1 - \mu)x_2}{R^3}$$

$$r = \{(x_1 - 1 + \mu)^2 + x_2^2\}^{1/2}$$

$$R = \{(x_1 + \mu)^2 + x_2^2\}^{1/2}$$

INPUT DATA DECK:

```
004
010
0.0
2.2234346E-04
2.2234346E-04
MU = .01215      $
SMR = (( Y1 - 1 + MU ) ** 2 + Y2 ** 2 ) ** .5   $
BGR = ( ( Y1 + MU ) ** 2 + Y2 ** 2 ) ** .5      $
D1 = Y3      $
D2 = Y4      $
D3 = 2 * Y4 + Y1 - MU * ( Y1 - 1 + MU ) / SMR ** 3 - ( 1 - MU ) *
      ( Y1 + MU ) / BGR ** 3      $
D4 = -2 * Y3 + Y2 - MU * Y2 / SMR ** 3 - ( 1 - MU ) * Y2 / BGR ** 3 $
-1.7641402E-02
-1.6018386E-02
9.8544878E 00
-4.1519712E 00
```

Output

The output will be as follows:

The equations will be printed as they were read in, followed by the list of initial conditions and their errors. Then for each printing interval, DELTAT, (specified on the fifth data card), the following will be printed: the real time elapsed since the last print statement, the total real time elapsed, T, the present value of the independent variable solution (s) at that value, and their associated errors.

Printing will stop when the solution at the final value of the independent variable TFINAL has been printed, see examples.

The following messages may occur:

SOLUTION IS A CONSTANT, when such is the case. When the solution is a polynomial - its coefficients will be printed. Delta T = 0 will be printed when a solution cannot be obtained at a given value of the independent value, and the program will terminate.

OUTPUT

Formulas compiled are

D1 = 2 * Y1 \$

Initial conditions at T = 0
Y1 = 1.000000000E 00
Solution at T = 1.000000000E-01
Y1 = 1.2214027582E 00
Solution at T = 2.000000000E-01
Y1 = 1.4918246976E 00
Solution at T = 3.000000000E-01
Y1 = 1.8221188004E 00
Solution at T = 4.000000000E-01
Y1 = 2.2255409285E 00
Solution at T = 5.000000000E-01
Y1 = 2.7182818284E 00
Solution at T = 6.000000000E-01
Y1 = 3.3201169228E 00
Solution at T = 7.000000000E-01
Y1 = 4.0551999670E 00
Solution at T = 8.000000000E-01
Y1 = 4.9530324248E 00
Solution at T = 9.000000000E-01
Y1 = 6.0496474648E 00
Solution at T = 1.000000000E 00
Y1 = 7.3890560995E 00

Error = 0
Time since last print = .63 seconds, total elapsed time = .63 seconds.
Error = 2.910E-11
Time since last print = .77 seconds, total elapsed time = 1.40 seconds.
Error = 5.821E-11
Time since last print = .75 seconds, total elapsed time = 2.15 seconds.
Error = 8.731E-11
Time since last print = .75 seconds, total elapsed time = 2.90 seconds.
Error = 1.164E-10
Time since last print = .77 seconds, total elapsed time = 3.67 seconds.
Error = 1.746E-10
Time since last print = 1.42 seconds, total elapsed time = 5.08 seconds.
Error = 2.910E-10
Time since last print = .75 seconds, total elapsed time = 5.83 seconds.
Error = 4.657E-10
Time since last print = .75 seconds, total elapsed time = 6.58 seconds.
Error = 5.821E-10
Time since last print = .77 seconds, total elapsed time = 7.35 seconds.
Error = 8.149E-10
Time since last print = .75 seconds, total elapsed time = 8.10 seconds.
Error = 1.048E-09

All printed output appearing in this report was obtained from the CDC 1604.

OUTPUT

Formulas compiled are

DI = Y1 ** 2 \$

```

Initial conditions at T =          0
Y1 = 1.000000000E 00
Solution at T = 1.0000000E-01      Time since last print = 5.70 seconds, total elapsed time = 5.70 seconds.
Y1 = 1.11111111E 00
Solution at T = 2.0000000E-01      Time since last print = 4.12 seconds, total elapsed time = 9.82 seconds.
Y1 = 1.250000000E 00
Solution at T = 3.0000000E-01      Time since last print = 5.47 seconds, total elapsed time = 15.28 seconds.
Y1 = 1.4285714286E 00
Solution at T = 4.0000000E-01      Time since last print = 5.47 seconds, total elapsed time = 20.75 seconds.
Y1 = 1.666666667E 00
Solution at T = 5.0000000E-01      Time since last print = 5.43 seconds, total elapsed time = 26.18 seconds.
Y1 = 2.000000001E 00
Solution at T = 6.0000000E-01      Time since last print = 8.18 seconds, total elapsed time = 34.37 seconds.
Y1 = 2.500000001E 00
Solution at T = 7.0000000E-01      Time since last print = 8.13 seconds, total elapsed time = 42.50 seconds.
Y1 = 3.333333335E 00
Solution at T = 8.0000000E-01      Time since last print = 12.18 seconds, total elapsed time = 54.68 seconds.
Y1 = 5.000000007E 00
Solution at T = 9.0000000E-01      Time since last print = 17.57 seconds, total elapsed time = 72.25 seconds.
Y1 = 1.000000003E 01
Delta T = 0

```

Error = 0
Error = 5.821E-11
Error = 1.455E-10
Error = 2.619E-10
Error = 4.366E-10
Error = 6.985E-10
Error = 1.339E-09
Error = 2.619E-09
Error = 6.519E-09
Error = 2.771E-08

OUTPUT

Formulas compiled are

```

MU = .01215 $
SMR = (( Y1 - 1 + MU ) ** 2 + Y2 ** 2 ) ** .5 $
BGR = (( Y1 - MU ) ** 2 + Y2 ** 2 ) ** .5 $
D1 = Y3 $
D2 = Y4 $
D3 = Y4 $
D3 = 2 * Y4 + Y1 - MU * (Y1 - 1 + MU) / SMR ** 3 - ( 1 - MU ) *
(Y1 + MU) / BGR ** 3 $
D4 = -2 * Y3 + Y2 - MU * Y2 / SMR ** 3 - ( 1 - MU ) * Y2 / BGR ** 3 $

```

Initial conditions at T =	0
Y1 = -1.9801200000E-02	Error = 0
Y2 = -1.5016200000E-02	Error = 0
Y3 = 9.5560067999E 00	Error = 0
Y4 = -4.8568780000E 00	Error = 0

Solution at T = 2.2234346E-04	Time since last print = 164.85 seconds, total elapsed time = 164.85 seconds.
Y1 = -1.7641401890E-02	Error = 9.095E-13
Y2 = -1.6018386585E-02	Error = 4.547E-13
Y3 = 9.8544877290E 00	Error = 6.985E-10
Y4 = -4.1519711651E 00	Error = 5.821E-10

Other Subroutines

The subroutine SEARCH has been omitted from the listing of DIFEQ because it is contained in the 1604 and 3600 libraries. Below is a listing of SEARCH if it is needed. It is a general table — lookup routine. The calling sequence is

CALL SEARCH (N, TABLE, ARG, IND), where:

N is the number of entries to be searched;

TABLE is the name of the array to be scanned;

ARG is the argument we are searching for;

IND is the output parameter, which contains the ordinal of the argument in the table; IND is zero if ARG is not in the table.

SUBROUTINE SEARCH (K, A, S, N)

TYPE INTEGER A, S

DIMENSION A(K)

DO 10 I = 1, K

IF (S. EQ. A(I)) 11, 10

10 CONTINUE

N = 0

RETURN

11 N = I

END

REFERENCE

1. Moore, R. E., "Interval Analysis", Prentice-Hall, 1966.

Listing of DIFEQ for the CDC 1604 may be obtained by writing to

Mathematics Research Center
University of Wisconsin
Madison, Wisconsin 53706

Following is the listing of DIFEQ for the CDC 3600.

```
PROGRAM DIFEQ DFQ 10
C THIS PROGRAM PRODUCES A NUMERICAL SOLUTION FOR A SYSTEM OF N DFQ 20
C FIRST-ORDER ORDINARY DIFFERENTIAL EQUATIONS WITH GIVEN DFQ 30
C INITIAL CONDITIONS. THE SYSTEM IS ASSUMED TO BE AUTONOMOUS. DFQ 40
C ERROR-BOUNDING IS RIGOROUS, COMPLETELY AUTOMATIC, AND INCLUDESDFQ 50
C ROUND-OFF ERRORS. METHOD OF SOLUTION IS BY EXPANSION IN A DFQ 60
C TAYLOR SERIES. COMPUTATION IS DONE USING INTERVAL ARITHMETIC. DFQ 70
C DFQ 80
C INPUT IS AS FOLLOWS. DFQ 90
C 1) N (SIZE OF THE SYSTEM) DFQ 100
C 2) NDER (NUMBER OF TERMS TO BE TAKEN IN THE TAYLOR EXPANSION) DFQ 110
C 3) TSTART (STARTING VALUE OF THE INDEPENDENT VARIABLE) DFQ 120
C 4) TFINAL (FINAL VALUE OF THE INDEPENDENT VARIABLE) DFQ 130
C 5) DELTAT (PRINTING INTERVAL - RESULT WILL BE PRINTED FOR EACH DFQ 140
C      INCREMENT OF DELTAT IN THE INDEPENDENT VARIABLE) DFQ 150
C 6) THE SYSTEM OF EQUATIONS, REPRESENTED BY FORTRAN-TYPE DFQ 160
C      STATEMENTS, EACH EQUATION TERMINATED BY $ DFQ 170
C 7) THE INITIAL CONDITIONS, GIVEN AS INTERVALS (DEGENERATE OR DFQ 180
C      OTHERWISE). DFQ 190
C DFQ 200
C DFQ 210
C
C TYPE IN5(2) Y,D,Q,T ,DELTAT,YOLD,PSEUDT,BBOX DFQ 220
C COMMON Y,D,Q,T,NSYS,NDER DFQ 230
C DIMENSION Y(31,12),D(31,12),Q(31,30),T(31,100),YOLD(31,12), DFQ 240
C BBOX(12),YYOLD(31) DFQ 250
C COMMON/OVERFLOW/INDCAT DFQ 260
C COMMON/YOLD/YOLD DFQ 270
C DIMENSION DT(2),YY(2,31,12),BB(2,12) DFQ 280
C EQUIVALENCE(DT,DELTAT),(DELT,DT(2)),(Y,YY),(BBOX,BB) DFQ 290
C DATA(DT=0.) DFQ 300
C DATA (TWOM36=1.455E-11) DFQ 310
C TYPE LOGICAL SW DFQ 320
C READ 1,NSYS,NDER DFQ 330
C 1 FORMAT(I3) DFQ 340
C ND1=NDER+1 DFQ 350
C READ 2,TSTART,TFINAL,PRINTDEL DFQ 360
C 2 FORMAT(E20.8) DFQ 370
C CALL COMPILE(NSYS,NDER) DFQ 380
C CALL ZCODEINT(Y,D,Q,T,62) DFQ 390
C READ 3,((YY(I2,1,I1),I2=1,2),I1=1,NSYS) DFQ 400
C 3 FORMAT((E20.8,E20.8)) DFQ 410
C DFQ 420
C
C INITIALIZATION DFQ 430
C DELT=POWER2(2.**(-36./(NDER-1))) DFQ 440
C IF(DELT.EQ.0) GO TO 500 DFQ 450
C CALL PRINSTAR(TSTART,PRINTDEL) DFQ 460
```

```

SW=0 DFQ 470
TIME=TSTART DFQ 480
C DFQ 490
C DFQ 500
C MAIN LOOP DFQ 510
C DFQ 520
C COMPUTE THE FIRST (NDER-1) DERIVATIVES AT Y=Y0 DFQ 530
100 CALL YSUPERK(NDER-1) DFQ 540
PSEUDT=0. DFQ 550
C OBTAIN NORM OF Y! DFQ 560
YNORM=FNORM(D,NSYS) DFQ 570
IF(YNORM.EQ.0) GO TO 500 DFQ 580
C SAVE THE VALUES OF Y0 DFQ 590
DO 110 J1=1,NDER DFQ 600
DO 110 K1=1,NSYS DFQ 610
110 YOLD(J1,K1)=Y(J1,K1) DFQ 620
C OBTAIN B-BOX DFQ 630
120 DO 130 K2=1,NSYS DFQ 640
Y(1,K2)=YOLD(1,K2)+YOLD(2,K2)*DELTAT/YNORM DFQ 650
130 BBOX(K2)=Y(1,K2) DFQ 660
C OBTAIN A-BOX DFQ 670
C DFQ 680
140 INDCAT=0 DFQ 690
CALL YSUPERK(NDER), DFQ 700
IF(INDCAT)150,160 DFQ 710
C DFQ 720
C CANNOT COMPUTE REMAINDER OVER B-BOX - HALVE B-BOX AND TRY AGAIN. DFQ 730
C DFQ 740
150 DELT=POWER2(DELT/2.) DFQ 750
IF(DELT.EQ.0) GO TO 500 DFQ 760
GO TO 120 DFQ 770
742 PRINT 743 DFQ 780
743 FORMAT(30X,30H THERE IS A POLYNOMIAL SOLUTION) DFQ 790
PRINT 744 DFQ 800
744 FORMAT(50X,*2 N*) DFQ 810
PRINT 745 DFQ 820
745 FORMAT(* THE POLY IS OF THE FORM P(X)=A0+A1(X-X0)+A2(X-X0) +.....+DFQ 830
XAN(X-X0) *) DFQ 840
PRINT 746, TIME DFQ 850
746 FORMAT(* WHERE X0=*F7.2) DFQ 860
PRINT 747 DFQ 870
747 FORMAT(* COEFF BELOW-CONSTANT TERM FIRST*)
748 IF(YOLD(NDER,1).NE.0) GO TO 749 DFQ 880
NDER=NDER-1 DFQ 890
GO TO 748 DFQ 900
749 DO 800 J=1,NDER DFQ 910
DFQ 920

```

```

800 YYOLD(J)=YOLD(J,1) DFQ 930
PRINT 750,(YYOLD(J),J=1,NDER) DFQ 940
750 FORMAT(5E20.8) DFQ 950
GO TO 500 DFQ 960
C DFQ 970
C COMPUTE A-BOX DFQ 980
160 CALL EXPAND(DELTAT) DFQ 990
C DFQ 1000
C TEST TO SEE IF A-BOX IS CONTAINED IN B-BOX DFQ 1010
DO 170 J3=1,NSYS DFQ 1020
IF((YY(1,1,J3).LT.BB(1,J3)).OR.(YY(2,1,J3).GT.BB(2,J3)))180,170 DFQ 1030
170 CONTINUE DFQ 1040
GO TO 300 DFQ 1050
C DFQ 1060
C A-BOX DOES NOT FIT INTO B-BOX -----TEST FLIP-FLOP DFQ 1070
180 IF(SW)190,200 DFQ 1080
C DFQ 1090
C PROCEDURE I (SW ON) ----- FLIP SWITCH, HALVE DELTAT, RE-EVALUATE ADFQ 1100
190 SW=0 DFQ 1110
DELT=POWER2(DELT/2.) DFQ 1120
IF(DELT.EQ.0) GO TO 500 DFQ 1130
GO TO 160 DFQ 1140
C DFQ 1150
C PROCEDURE II (SW OFF) ----- FLIP SW, REPLACE B BY A, COMPUTE DELT DFQ 1160
200 SW=1 DFQ 1170
C OBTAIN WIDTH OF YSUPERK(B) DFQ 1180
WIDTHB=0. DFQ 1190
DO 210 I3=1,NSYS DFQ 1200
210 WIDTHB=MAX1F(WIDTHB,YY(2,NDER+1,I3)-YY(1,NDER+1,I3)) DFQ 1210
IF(WIDTHB.EQ.0) GO TO 742 DFQ 1220
C OBTAIN WIDTH OF YSUPERK(A) DFQ 1230
INDCAT=0 DFQ 1240
CALL YSUPERK(NDER) DFQ 1250
IF(INDCAT)150,220 DFQ 1260
220 WIDTHA=0. DFQ 1270
DO 230 K3=1,NSYS DFQ 1280
230 WIDTHA=MAX1F(WIDTHA,YY(2,NDER+1,K3)-YY(1,NDER+1,K3)) DFQ 1290
IF(WIDTHA.EQ.0) GO TO 742 DFQ 1300
C OBTAIN FUDGE-INTEGER D DFQ 1310
KD=MAX1F(0.,(LOGF(WIDTHB)-LOGF(WIDTHA))/LOGF(DELT)) DFQ 1320
C COMPUTE NEW DELT DFQ 1330
EXPFUD=1./FLOATF(KD+NDER-1) DFQ 1340
DELT=POWER2((TWOM36*YNORM/WIDTHB)**EXPFUD) DFQ 1350
IF(DELT.EQ.0) GO TO 500 DFQ 1360
C SAVE B-BOX (THAT WAS A-BOX) DFQ 1370
DO 240 I4=1,NSYS DFQ 1380

```

```

240 BBOX(I4)=Y(1,I4) DFQ 1390
GO TO 160 DFQ 1400
C DFQ 1410
C SUCCESSFUL BOUNDING OF REMAINDER ----- FINISH UP DFQ 1420
C ----- GET BETTER BOUND ON REMAINDER TERM DFQ 1430
300 CALL YSUPERK(NDER) DFQ 1440
C ----- TEST FOR PRINTING (PRINT) DFQ 1450
CALL PRINTER(TIME,DELT) DFQ 1460
C STEP INDEPENDENT VARIABLE, AND TEST FOR END DFQ 1470
310 TIME=TIME+DELT DFQ 1480
IF(TIME.GE.TFINAL)500,320 DFQ 1490
C OBTAIN NEW BASE POINT Y0 DFQ 1500
320 PSEUDT=DELT DFQ 1510
CALL EXPAND (PSEUDT) DFQ 1520
GO TO 100 DFQ 1530
C DFQ 1540
C END DFQ 1550
500 CONTINUE DFQ 1560
END DFQ 1570
SUBROUTINE YSUPERK(NDER) DFQ 1580
TYPE INT5(2) Y,D,Q,T DFQ 1590
COMMON Y(31,12),D(31,12),Q(31,30),T(31,100),N,K DFQ 1600
DO 1 J=1,NDER DFQ 1610
CALL DECODINT(J-1) DFQ 1620
DO 1 I=1,N DFQ 1630
1 Y(J+1,I)=D(J,I)/J DFQ 1640
END DFQ 1650
SUBROUTINE EXPAND(T) DFQ 1660
TYPE INT5(2) Y,YOLD,T DFQ 1670
COMMON Y(31,12),OTHER(8804),NSYS,NDER DFQ 1680
COMMON/YOLD/YOLD(31,12) DFQ 1690
DO 1 I=1,NSYS DFQ 1700
Y(1,I)=Y(NDER+1,I) DFQ 1710
DO 1 J=1,NDER DFQ 1720
M=NDER-J+1 DFQ 1730
1 Y(1,I)=Y(1,I)*T+YOLD(M,I) DFQ 1740
END DFQ 1750
SUBROUTINE PRINTER(TIME,DELT) DFQ 1760
TYPE INT5(2) Y,PSEUDT DFQ 1770
COMMON Y(31,12),OTHER(8804),NSYS,NDER DFQ 1780
DIMENSION YY(2,31,12) DFQ 1790
EQUIVALENCE(Y,YY) DFQ 1800
KS=1 DFQ 1810
2 IF(TIME+DELT.GE.TLASTPR+PRDELT)1,100 DFQ 1820
1 TLASTPR=TLASTPR+PRDELT DFQ 1830
CURT=TIMEF(DUMMY) DFQ 1840

```

```

ELT=(CURT-RTPL)/1000. DFQ 1850
TEL=(CURT-RTIME)/1000. DFQ 1860
RTPL=CURT DFQ 1870
PSEUDT=TLASTPR-TIME DFQ 1880
CALL EXPAND(PSEUDT) DFQ 1890
PRINT 10,TLASTPR,ELT,TEL DFQ 1900
10 FORMAT(15HOSOLUTION AT T=E15.7,5X,23HTIME SINCE LAST PRINT =F6.2, DFQ 1910
1 31H SECONDS, TOTAL ELAPSED TIME = F7.2,9H SECONDS.) DFQ 1920
50 DO 60 I=1,NSYS DFQ 1930
  X=Y(1,I)
  E=YY(2,1,I)-X DFQ 1940
  PRINT 51,I,X,E DFQ 1950
51 FORMAT(10X,1HY,I2,4X,1H=,E20.10,20X,7HERROR =E13.3) DFQ 1970
60 CONTINUE DFQ 1980
  GO TO(2,100),KS DFQ 1990
100 RETURN DFQ 2000
  ENTRY PRINSTAR DFQ 2010
  KS=2 DFQ 2020
  TLASTPR=TIME DFQ 2030
  PRDELT=DELT DFQ 2040
  PRINT 61,TIME DFQ 2050
61 FORMAT(27HO INITIAL CONDITIONS AT T = F15.10) DFQ 2060
  RTIME=RTPL=TIMEF(DUMMY) DFQ 2070
  GO TO 50 DFQ 2080
  END DFQ 2090
  FUNCTION FNORM(D,N) DFQ 2100
  DIMENSION D(2,31,12) DFQ 2110
  FNORM=0. DFQ 2120
  DO 1 I=1,N DFQ 2130
1 FNORM=MAX1F(FNORM,ABSF(D(1,1,I)),ABSF(D(2,1,I))) DFQ 2140
  IF(FNORM.EQ.0.)2,10 DFQ 2150
2 PRINT 3 DFQ 2160
3 FORMAT(22HOSOLUTION IS CONSTANT.) DFQ 2170
10 RETURN DFQ 2180
  END DFQ 2190
  FUNCTION POWER2(A) DFQ 2200
  DATA(TWO20=2025400000000000B) DFQ 2210
  TYPE INTEGER Q DFQ 2220
  Q=A*TWO20 DFQ 2230
  IF(Q)10,1 DFQ 2240
1 PRINT 2 DFQ 2250
2 FORMAT(13HO DELTA T = 0) DFQ 2260
  POWER2=0 $ RETURN DFQ 2270
10 POWER2=FLOATF(Q)/TWO20 DFQ 2280
  END DFQ 2290
  SUBROUTINE ZCODEINT(Z,D,Q,T,KSTOR) DFQ 2300

```

```

DIMENSION Z(1),D(1),Q(1),T(1) DFQ 2310
COMMON/ZLIST/ZCODE(1000) DFQ 2320
COMMON/CONSTANT/C(51) DFQ 2330
COMMON/ERASABLE/MCODE(60),LEX(31),KC,LCOM(300),LCVM(300), DFQ 2340
1 LIBFUN(10),MORE(270),KTST DFQ 2350
TYPE INTEGER ZCODE,ZC,SWL,SWR,OP,E,RV DFQ 2360
DATA(MH=777777700000000B),(ML=7777777B),(LS8=100000000B) DFQ 2370
1 (LBLANK=60606060B) DFQ 2380
ZC=0 DFQ 2390
KSIN=KTST DFQ 2400
CALL STARTINT DFQ 2410
DO 500 ND=1,KC DFQ 2420
LV=LCVM(ND).AND.MH DFQ 2430
RV=LCVM(ND).AND.ML DFQ 2440
LV=LV/LS8 DFQ 2450
E=LCOM(ND).AND.ML DFQ 2460
NE=NAD(E,Z,D,Q,T,KSTOR) DFQ 2470
OP=LCOM(ND).AND.MH DFQ 2480
SWL=LV=LV.AND.ML DFQ 2490
IF(SWL.EQ.4R) 18,9 DFQ 2500
8 SWL=0 DFQ 2510
GO TO 10 DFQ 2520
9 SWL=SWL.AND.77B DFQ 2530
SWL=SWL-23B DFQ 2540
NL=NAD(LV,Z,D,Q,T,KSTOR) DFQ 2550
10 SWR=LCVM(ND).AND.77B DFQ 2560
SWR=SWR-23B DFQ 2570
NR=NAD(RV,Z,D,Q,T,KSTOR) DFQ 2580
ZC=ZC+1 DFQ 2590
CALL SEARCH(2,LIBFUN,10,IND,OP) DFQ 2600
IF(IND)20,11 DFQ 2610
11 CALL ERDIF DFQ 2620
STOP DFQ 2630
20 GO TO(110,120,130,140,150,160,170,180,190,200),IND DFQ 2640
C DFQ 2650
C ADDITION DFQ 2660
110 IF(SWL)111,115 DFQ 2670
C LDA(INTERVAL) 2 NL DFQ 2680
111 ZCODE(ZC)=MCODE(29) DFQ 2690
ZC=ZC+1 DFQ 2700
ZCODE(ZC)=MCODE(3)+NL DFQ 2710
IF(SWR)112,113 DFQ 2720
112 ZC=ZC+1 DFQ 2730
C FAD(INTERVAL) 2 NR DFQ 2740
ZCODE(ZC)=MCODE(18) DFQ 2750
ZC=ZC+1 DFQ 2760

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	ZCODE(ZC)=MCODE(3)+NR	DFQ 2770
119	ZC=ZC+1	DFQ 2780
C	STA 2 NE	DFQ 2790
	ZCODE(ZC)=MCODE(19)	DFQ 2800
	ZC=ZC+1	DFQ 2810
	ZCODE(ZC)=MCODE(3)+NE	DFQ 2820
	GO TO 490	DFQ 2830
113	ZC=ZC+1	DFQ 2840
C	LIU 1 (J) IJP 1 *+3	DFQ 2850
	ZCODE(ZC)=KRAMDN(MCODE(30),ZCODE(ZC+3))	DFQ 2860
1131	ZC=ZC+1	DFQ 2870
C	FAD(REAL) NR	DFQ 2880
	ZCODE(ZC)=MCODE(31)	DFQ 2890
	ZC=ZC+1	DFQ 2900
	ZCODE(ZC)=MCODE(4)+NR	DFQ 2910
	GO TO 119	DFQ 2920
115	IF(SWR)116,1119	DFQ 2930
1119	NT=NR	DFQ 2940
	NR=NL	DFQ 2950
	NL=NT	DFQ 2960
	GO TO 260	DFQ 2970
C	LDA(INTERVAL) NR	DFQ 2980
116	ZCODE(ZC)=MCODE(29)	DFQ 2990
	ZC=ZC+1	DFQ 3000
	ZCODE(ZC)=MCODE(3)+NR	DFQ 3010
	NR=NL	DFQ 3020
	IF(LV.EQLBLANK)119,113	DFQ 3030
118	IF(LV.EQLBLANK)1181,1131	DFQ 3040
1181	ZCODE(ZC-1)=ZCODE(ZC-1)-2	DFQ 3050
	GO TO 119	DFQ 3060
C	SUBTRACTION	DFQ 3070
120	IF(SWL)121,125	DFQ 3080
C	LDA(INTERVAL)2 NL	DFQ 3090
121	ZCODE(ZC)=MCODE(29)	DFQ 3100
	ZC=ZC+1	DFQ 3110
	ZCODE(ZC)=MCODE(3)+NL	DFQ 3120
	IF(SWR)122,123	DFQ 3130
122	ZC=ZC+1	DFQ 3140
C	FSB(INTERVAL) 2 NR	DFQ 3150
	ZCODE(ZC)=MCODE(32)	DFQ 3160
	ZC=ZC+1	DFQ 3170
	ZCODE(ZC)=MCODE(3)+NR	DFQ 3180
	GO TO 119	DFQ 3190
123	ZC=ZC+1	DFQ 3200
C	LIU 1 (J) IJP 1 *+3	DFQ 3210
		DFQ 3220

	ZCODE(ZC)=KRAMON(MCODE(30),ZCODE(ZC+3))	DFQ 3230
1231	ZC=ZC+1	DFQ 3240
C	FSB (REAL) NR	DFQ 3250
	ZCODE(ZC)=MCODE(33)	DFQ 3260
	ZC=ZC+1	DFQ 3270
	ZCODE(ZC)=MCODE(4)+NR	DFQ 3280
	GO TO 119	DFQ 3290
125	IF(SWR)126,260	DFQ 3300
C	LAC(INTERVAL) 2 NR	DFQ 3310
126	ZCODE(ZC)=MCODE(58)	DFQ 3320
	ZC=ZC+1	DFQ 3330
	ZCODE(ZC)=MCODE(3)+NR	DFQ 3340
	NR=NL	DFQ 3350
	IF (LV .EQ. LBLANK) 119,113	DFQ 3360
C	LAC(REAL) NR	DFQ 3370
128	ZCODE(ZC-1)=MCODE(12)	DFQ 3380
	ZCODE(ZC)=MCODE(4)+NR	DFQ 3390
	NR=NL	DFQ 3400
	IF(LV.EQ.LBLANK)1181,1131	DFQ 3410
C	MULTIPLICATION	DFQ 3420
130	IF(SWL)131,135	DFQ 3430
131	IF(SWR)132,133	DFQ 3440
132	KSW1=0	DFQ 3450
	SW2=1.	DFQ 3460
	KSW3=MCODE(23)	DFQ 3470
	KSW5=0	DFQ 3480
	ZCODE(ZC)=MCODE(49)	DFQ 3490
	GO TO 250	DFQ 3500
C	LDA (REAL) NR	DFQ 3510
133	ZCODE(ZC)=MCODE(28)	DFQ 3520
	ZC=ZC+1	DFQ 3530
	ZCODE(ZC)=MCODE(4)+NR	DFQ 3540
134	ZC=ZC+1	DFQ 3550
C	FMU(INTERVAL)2 NL	DFQ 3560
	ZCODE(ZC)=MCODE(34)	DFQ 3570
	ZC=ZC+1	DFQ 3580
	ZCODE(ZC)=MCODE(3)+NL	DFQ 3590
	GO TO 119	DFQ 3600
135	IF(SWR)136,260	DFQ 3610
136	NTEMP=NL	DFQ 3620
	NL=NR	DFQ 3630
	NR=NTEMP	DFQ 3640
	GO TO 133	DFQ 3650
138	ZC=ZC+1	DFQ 3660
C	FMU (REAL) NR	DFQ 3670
		DFQ 3680

ZCODE(ZC)=MCODE(35)	DFQ 3690
ZC=ZC+1	DFQ 3700
ZCODE(ZC)=MCODE(4)+NR	DFQ 3710
GO TO 119	DFQ 3720
C	DFQ 3730
C DIVISION	DFQ 3740
140 IF(SWR)141,146	DFQ 3750
C LIL 1 (2J) IJP 1 *+1	DFQ 3760
141 ZCODE(ZC)=KRAMDN(MCODE(36),ZCODE(ZC+1))	DFQ 3770
ZC=ZC+1	DFQ 3780
C IJP 1 *+4	DFQ 3790
ZCODE(ZC)=KRAMUP(MCODE(37),ZCODE(ZC+4))	DFQ 3800
ZC=ZC+1	DFQ 3810
KSW1=0	DFQ 3820
SW2=0	DFQ 3830
KSW3=MCODE(23)	DFQ 3840
KSW5=2	DFQ 3850
IF(SWL)142,143	DFQ 3860
C LDA (INTERVAL) NL	DFQ 3870
142 ZCODE(ZC)=MCODE(29)	DFQ 3880
ZC=ZC+1	DFQ 3890
ZCODE(ZC)=MCODE(3)+NL	DFQ 3900
ZC=ZC+1	DFQ 3910
C SLJ *+16	DFQ 3920
ZCODE(ZC)=KRAMUP(MCODE(38),ZCODE(ZC+16))	DFQ 3930
NTEMP=NL	DFQ 3940
NL=NE	DFQ 3950
GO TO 250	DFQ 3960
C LDA (REAL) NL	DFQ 3970
143 ZCODE(ZC)=MCODE(28)	DFQ 3980
ZC=ZC+1	DFQ 3990
ZCODE(ZC)=MCODE(4)+NL	DFQ 4000
ZC=ZC+1	DFQ 4010
C SLJ *+14	DFQ 4020
ZCODE(ZC)=KRAMUP(MCODE(38),ZCODE(ZC+14))	DFQ 4030
NL=NE	DFQ 4040
GO TO 250	DFQ 4050
145 IF(SWL)1451,1452	DFQ 4060
1451 ZC=ZC+1	DFQ 4070
C FAD (INTERVAL) 2 NL	DFQ 4080
ZCODE(ZC)=MCODE(18)	DFQ 4090
ZC=ZC+1	DFQ 4100
ZCODE(ZC)=MCODE(3)+NTEMP	DFQ 4110
1452 ZC=ZC+1	DFQ 4120
C FDV (INTERVAL) NR	DFQ 4130
ZCODE(ZC)=MCODE(39)	DFQ 4140

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ZC=ZC+1 DFQ 4150
ZCODE(ZC)=MCODE(4)+NR DFQ 4160
GO TO 119 DFQ 4170
146 IF(SWL)147,260 DFQ 4180
147 ZC=ZC+1 DFQ 4190
C LDA (INTERVAL) 2 NL DFQ 4200
ZCODE(ZC)=MCODE(29) DFQ 4210
ZC=ZC+1 DFQ 4220
ZCODE(ZC)=MCODE(3)+NL DFQ 4230
148 ZC=ZC+1 DFQ 4240
C FDV (REAL) NR DFQ 4250
ZCODE(ZC)=MCODE(40) DFQ 4260
ZC=ZC+1 DFQ 4270
ZCODE(ZC)=MCODE(4)+NR DFQ 4280
GO TO 119 DFQ 4290
C DFQ 4300
C X**Y, WHERE Y IS CONSTANT DFQ 4310
150 IF(SWL)152,260 DFQ 4320
152 K2=RV/100B DFQ 4330
EXPON=C(K2) DFQ 4340
KEX=EXPON DFQ 4350
EXPIT=KEX DFQ 4360
IF((EXPON.EQ.EXPIT).AND.(KEX.GE.0))155,151 DFQ 4370
155 IF(KEX-1)1591,1592,156 DFQ 4380
156 SWK=0 DFQ 4390
NP=NL DFQ 4400
NET=NE DFQ 4410
157 KET=KEX DFQ 4420
KEX=KEX/2 DFQ 4430
IF(KET.EQ.KEX*2)1576,1571 DFQ 4440
1571 IF(SWK)1572,1575 DFQ 4450
1572 NL=NP DFQ 4460
NR=NY1 DFQ 4470
IF(KEX)1573,1574 DFQ 4480
1573 KSIN=KSIN+1 DFQ 4490
K1=(KSIN-1)*KSTOR+1 DFQ 4500
NE=NY1=KRAMDN(0,T(K1)) DFQ 4510
IND=1 DFQ 4520
GO TO 132 DFQ 4530
1574 NE=NET DFQ 4540
IND=3 DFQ 4550
GO TO 132 DFQ 4560
1575 NY1=NP DFQ 4570
SWK=1. DFQ 4580
GO TO 1576 DFQ 4590
1576 NL=NR=NP DFQ 4600

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IF((KEX.EQ.1).ANU.(SWK.EQ.0.))1574,1577 DFQ 4610
1577 KSIN=KSIN+1 DFQ 4620
    K1=(KSIN-1)*KSTOR+1 DFQ 4630
    NE=NP=KRAMDN(0,T(K1)) DFQ 4640
    IND=2 DFQ 4650
    GO TO 132 DFQ 4660
1591 NL=KRAMDN(0,C(2)) DFQ 4670
    IND=1 DFQ 4680
    LV=LBLANK DFQ 4690
    GO TO 260 DFQ 4700
1592 LV=LBLANK DFQ 4710
    NR=NL DFQ 4720
    GO TO 116 DFQ 4730
C   LIL 1 (2J) IJP 1 *+6 DFQ 4740
151 ZCODE(ZC)=KRAMDN(MCODE(36),ZCODE(ZC+6)) DFQ 4750
    ZC=ZC+1 DFQ 4760
C   ISK 0 ZRO X DFQ 4770
    ZCODE(ZC)=MCODE(41) DFQ 4780
    ZC=ZC+1 DFQ 4790
    ZCODE(ZC)=KRAMUP(MCODE(38),ZCODE(ZC+3)) DFQ 4800
    ZC=ZC+1 DFQ 4810
C   RTJ(EXPRAL) ZRO Y DFQ 4820
    ZCODE(ZC)=MCODE(4)+NL DFQ 4830
    ZC=ZC+1 DFQ 4840
    ZCODE(ZC)=MCODE(4)+NR DFQ 4850
    ZC=ZC+1 DFQ 4860
C   SLJ *+17 DFQ 4870
    ZCODE(ZC)=KRAMUP(MCODE(38),ZCODE(ZC+17)) DFQ 4880
    ZC=ZC+1 DFQ 4890
C   RTJ COM3 ZRO NR DFQ 4900
    ZCODE(ZC)=MCODE(42)+NR DFQ 4910
    KSW1=0 DFQ 4920
    SW2=1 DFQ 4930
    KSW3=MCODE(22) DFQ 4940
    KSW5=2 DFQ 4950
    NR=NL DFQ 4960
    NL=NE DFQ 4970
    GO TO 250 DFQ 4980
158 ZCODE(ZC-1)=MCODE(43)+NL DFQ 4990
    ZCODE(ZC-2)=ZCODE(ZC-2)-2 DFQ 5000
    ZCODE(ZC)=NR DFQ 5010
    GO TO 119 DFQ 5020
C   Z=LOG(X) DFQ 5030
C   160 IF(SWR)161,260 DFQ 5040
C   LIL 1 (2J) IJP 1 *+1 DFQ 5050
                                         DFQ 5060

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161 ZCODE(ZC)=KRAMDN(MCODE(36),ZCODE(ZC+1)) DFQ 5070
    ZC=ZC+1 DFQ 5080
    C IJP 1 *#7 DFQ 5090
    ZCODE(ZC)=KRAMUP(MCODE(37),ZCODE(ZC+7)) DFQ 5100
    ZC=ZC+1 DFQ 5110
    C RTJ LOG5 DFQ 5120
    ZCODE(ZC)=MCODE(7) DFQ 5130
    ZC=ZC+1 DFQ 5140
    C SLJ *+2 DFQ 5150
    ZCODE(ZC)=KRAMUP(MCODE(38),ZCODE(ZC+2)) DFQ 5160
    ZC=ZC+1 DFQ 5170
    C DLDA X DFQ 5180
    ZCODE(ZC)=MCODE(4)+NR DFQ 5190
    ZC=ZC+1 DFQ 5200
    C STA(INTERVAL) 2 Z DFQ 5210
    ZCODE(ZC)=MCODE(19) DFQ 5220
    ZC=ZC+1 DFQ 5230
    ZCODE(ZC)=MCODE(4)+NE DFQ 5240
    ZC=ZC+1 DFQ 5250
    C SLJ *+25 DFQ 5260
    ZCODE(ZC)=KRAMUP(MCODE(38),ZCODE(ZC+25)) DFQ 5270
    ZC=ZC+1 DFQ 5280
    C IJP 1 *+4 PASS DFQ 5290
    ZCODE(ZC)=KRAMUP(MCODE(37),ZCODE(ZC+4)) DFQ 5300
    ZC=ZC+1 DFQ 5310
    C LDA (INTERVAL) 2 X DFQ 5320
    ZCODE(ZC)=MCODE(29) DFQ 5330
    ZC=ZC+1 DFQ 5340
    ZCODE(ZC)=MCODE(3)+NR DFQ 5350
    ZC=ZC+1 DFQ 5360
    C SLJ *+17 DFQ 5370
    ZCODE(ZC)=KRAMUP(MCODE(38),ZCODE(ZC+17)) DFQ 5380
    ZC=ZC+1 DFQ 5390
    C ENI 4 0 INI 1 -1 DFQ 5400
    ZCODE(ZC)=MCODE(50) DFQ 5410
    KSW1=2 DFQ 5420
    SW2=0 DFQ 5430
    KSW3=MCODE(21) DFQ 5440
    KSW5=2 DFQ 5450
    NL=NR DFQ 5460
    NTEMP=NR DFQ 5470
    NR=NE DFQ 5480
    GO TO 250 DFQ 5490
164 NR=NL DFQ 5500
    GO TO 1451 DFQ 5510
    C LDA X STA T+1 DFQ 5520

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168	ZCODE(ZC-1)=MCODE(45)+NR*LS8	DFQ 5530
	ZCODE(ZC-2)=ZCODE(ZC-2)+1	DFQ 5540
C	STA T+2	DFQ 5550
	ZCODE(ZC)=MCODE(46)	DFQ 5560
	ZC=ZC+1	DFQ 5570
C	RTJ LOG5 (OR EXP5,SIN5,COS5,ATAN5)	DFQ 5580
	ZCODE(ZC)=MCODE(1+IND)	DFQ 5590
	ZC=ZC+1	DFQ 5600
C	SLJ *+2	DFQ 5610
	ZCODE(ZC)=KRAMUP(MCODE(38),ZCODE(ZC+2))	DFQ 5620
	ZC=ZC+1	DFQ 5630
C	DLDA T+1	DFQ 5640
	ZCODE(ZC)=MCODE(4)+T+1	DFQ 5650
	ZC=ZC+1	DFQ 5660
C	STA(INTERVAL) Z	DFQ 5670
	ZCODE(ZC)=MCODE(19)	DFQ 5680
	ZC=ZC+1	DFQ 5690
	ZCODE(ZC)=MCODE(4)+NE	DFQ 5700
	GO TO 490	DFQ 5710
C		DFQ 5720
C	Z=EXPF(X)	DFQ 5730
170	IF(SWR)171,260	DFQ 5740
C	LIL 1 (2J) IJP 1 *+1	DFQ 5750
171	ZCODE(ZC)=KRAMUN(MCODE(36),ZCODE(ZC+1))	DFQ 5760
	ZC=ZC+1	DFQ 5770
C	IJP 1 *+7	DFQ 5780
	ZCODE(ZC)=KRAMUP(MCODE(37),ZCODE(ZC+7))	DFQ 5790
	ZC=ZC+1	DFQ 5800
C	RTJ EXP5	DFQ 5810
	ZCODE(ZC)=MCODE(8)	DFQ 5820
	ZC=ZC+1	DFQ 5830
C	SLJ *+2	DFQ 5840
	ZCODE(ZC)=KRAMUP(MCODE(38),ZCODE(ZC+2))	DFQ 5850
	ZC=ZC+1	DFQ 5860
	DLDA X	DFQ 5870
	ZCODE(ZC)=MCODE(4)+NR	DFQ 5880
	ZC=ZC+1	DFQ 5890
C	STA(INTERVAL) Z	DFQ 5900
	ZCODE(ZC)=MCODE(19)	DFQ 5910
	ZC=ZC+1	DFQ 5920
	ZCODE(ZC)=MCODE(4)+NE	DFQ 5930
	ZC=ZC+1	DFQ 5940
C	SLJ *+15	DFQ 5950
	ZCODE(ZC)=KRAMUP(MCODE(38),ZCODE(ZC+15))	DFQ 5960
	ZC=ZC+1	DFQ 5970
C	ENI 4 0 PASS	DFQ 5980

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ZCODE(ZC)=MCODE(44) DFQ 5990
KSW1=0 DFQ 6000
SW2=1. DFQ 6010
KSW3=MCODE(21) DFQ 6020
KSW5=2 DFQ 6030
NL=NE DFQ 6040
GO TO 250 DFQ 6050
C DFQ 6060
C Z=SINF(X) DFQ 6070
180 IF(SWR)181,260 DFQ 6080
181 KSIN=KSIN+1 DFQ 6090
    K1=(KSIN-1)*KSTOR+1 DFQ 6100
    NW=KRAMDN(0,T(K1)) DFQ 6110
C LIL 1 (2J) IJP 1 *+1 DFQ 6120
182 ZCODE(ZC)=KRAMDN(MCODE(36),ZCODE(ZC+1)) DFQ 6130
    ZC=ZC+1 DFQ 6140
C IJP 1 *+12 DFQ 6150
    ZCODE(ZC)=KRAMUP(MCODE(37),ZCODE(ZC+12)) DFQ 6160
    ZC=ZC+1 DFQ 6170
C RTJ SIN5 DFQ 6180
    ZCODE(ZC)=MCODE(9) DFQ 6190
    ZC=ZC+1 DFQ 6200
C SLJ *+2 DFQ 6210
    ZCODE(ZC)=KRAMUP(MCODE(38),ZCODE(ZC+2)) DFQ 6220
    ZC=ZC+1 DFQ 6230
C DLDA X DFQ 6240
    ZCODE(ZC)=MCODE(4)+NR DFQ 6250
    ZC=ZC+1 DFQ 6260
C STA(INTERVAL) Z DFQ 6270
    ZCODE(ZC)=MCODE(19) DFQ 6280
    ZC=ZC+1 DFQ 6290
    ZCODE(ZC)=MCODE(4)+NE DFQ 6300
    ZC=ZC+1 DFQ 6310
C RTJ COS5 DFQ 6320
    ZCODE(ZC)=MCODE(10) DFQ 6330
    ZC=ZC+1 DFQ 6340
C SLJ *+2 DFQ 6350
    ZCODE(ZC)=KRAMUP(MCODE(38),ZCODE(ZC+2)) DFQ 6360
    ZC=ZC+1 DFQ 6370
C DLDA X DFQ 6380
    ZCODE(ZC)=MCODE(4)+NR DFQ 6390
    ZC=ZC+1 DFQ 6400
C STA(INTERVAL) Z DFQ 6410
    ZCODE(ZC)=MCODE(19) DFQ 6420
    ZC=ZC+1 DFQ 6430
    ZCODE(ZC)=MCODE(4)+NW DFQ 6440

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C   ZC=ZC+1                               DFQ 6450
    SLJ *+29                               DFQ 6460
    ZCODE(ZC)=KRAMUP(MCODE(38),ZCODE(ZC+29)) DFQ 6470
    ZC=ZC+1                               DFQ 6480
C   ENI 4 0      PASS                      DFQ 6490
    ZCODE(ZC)=MCODE(44)                    DFQ 6500
    KSW1=0                                DFQ 6510
    SW2=1.                                DFQ 6520
    KSW3=MCODE(21)                        DFQ 6530
    KSW5=2                                DFQ 6540
    NL=NW                                 DFQ 6550
    GO TO 250                            DFQ 6560
185  IND=IND+1                           DFQ 6570
    SW2=0.                                DFQ 6580
    NL=NE                                 DFQ 6590
    NE=NW                                 DFQ 6600
    ZC=ZC+1                               DFQ 6610
C   ENI 4 0      LIL 1 (2J-2)             DFQ 6620
    ZCODE(ZC)=MCODE(47)                    DFQ 6630
    GO TO 250                            DFQ 6640
C   Z=COSF(X)                           DFQ 6650
190  IF(SWR)191,260                     DFQ 6660
191  NW=NE                               DFQ 6670
    KSIN=KSIN+1                          DFQ 6680
    K1=(KSIN-1)*KSTOR+1                  DFQ 6690
    NE=KRAMDN(0,T(K1))                  DFQ 6700
    IND=IND-1                           DFQ 6710
    GO TO 182                           DFQ 6720
DFQ 6730
C   Z=ATAN(X)                           DFQ 6740
200  IF(SWR)201,260                     DFQ 6750
201  KSIN=KSIN+1                          DFQ 6760
    K1=(KSIN-1)*KSTOR+1                  DFQ 6770
    NV=KRAMDN(0,T(K1))                  DFQ 6780
    KSIN=KSIN+1                          DFQ 6790
    K1=(KSIN-1)*KSTOR+1                  DFQ 6800
    NW=KRAMDN(0,T(K1))                  DFQ 6810
DFQ 6820
C   LIL 1 (2J)          IJP 1  **1        DFQ 6830
    ZCODE(ZC)=KRAMDN(MCODE(36),ZCODE(ZC+1)) DFQ 6840
    ZC=ZC+1                               DFQ 6850
C   IJP 1  **21                         DFQ 6860
    ZCODE(ZC)=KRAMUP(MCODE(37),ZCODE(ZC+21)) DFQ 6870
    ZC=ZC+1                               DFQ 6880
C   RTJ ATAN5                           DFQ 6890
    ZCODE(ZC)=MCODE(11)                    DFQ 6900

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    ZC=ZC+1 DFQ 6910
C   SLJ *+2 DFQ 6920
ZCODE(ZC)=KRAMUP(MCODE(38),ZCODE(ZC+2)) DFQ 6930
ZC=ZC+1 DFQ 6940
C   DLDA X DFQ 6950
ZCODE(ZC)=MCODE(4)+NR DFQ 6960
ZC=ZC+1 DFQ 6970
C   STA(INTERVAL) Z DFQ 6980
ZCODE(ZC)=MCODE(19) DFQ 6990
ZC=ZC+1 DFQ 7000
ZCODE(ZC)=MCODE(4)+NE DFQ 7010
ZC=ZC+1 DFQ 7020
C   LDA (INTERVAL) X DFQ 7030
ZCODE(ZC)=MCODE(29) DFQ 7040
ZC=ZC+1 DFQ 7050
ZCODE(ZC)=MCODE(3)+NR DFQ 7060
ZC=ZC+1 DFQ 7070
C   FMU(INTERVAL) X DFQ 7080
ZCODE(ZC)=MCODE(34) DFQ 7090
ZC=ZC+1 DFQ 7100
ZCODE(ZC)=MCODE(3)+NR DFQ 7110
ZC=ZC+1 DFQ 7120
C   FAD (REAL) 1. DFQ 7130
ZCODE(ZC)=MCODE(31) DFQ 7140
ZC=ZC+1 DFQ 7150
ZCODE(ZC)=MCODE(4)+1 DFQ 7160
ZC=ZC+1 DFQ 7170
C   STA V DFQ 7180
ZCODE(ZC)=MCODE(19) DFQ 7190
ZC=ZC+1 DFQ 7200
ZCODE(ZC)=MCODE(3)+NV DFQ 7210
ZC=ZC+1 DFQ 7220
C   LDA (REAL) 1. DFQ 7230
ZCODE(ZC)=MCODE(28) DFQ 7240
ZC=ZC+1 DFQ 7250
ZCODE(ZC)=MCODE(4)+1 DFQ 7260
ZC=ZC+1 DFQ 7270
C   FDV (INTERVAL) V DFQ 7280
ZCODE(ZC)=MCODE(39) DFQ 7290
ZC=ZC+1 DFQ 7300
ZCODE(ZC)=MCODE(4)+NV DFQ 7310
ZC=ZC+1 DFQ 7320
C   STA W DFQ 7330
ZCODE(ZC)=MCODE(19) DFQ 7340
ZC=ZC+1 DFQ 7350
ZCODE(ZC)=MCODE(3)+NW DFQ 7360

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C	ZC=ZC+1	DFQ 7370
	SLJ *+47	DFQ 7380
	ZCODE(ZC)=KRAMUP(MCODE(38),ZCODE(ZC+47))	DFQ 7390
C	ZC=ZC+1	DFQ 7400
C	INI 1 2 PASS	DFQ 7410
	ZCODE(ZC)=MCODE(48)	DFQ 7420
	NT=NE	DFQ 7430
	NL=NR	DFQ 7440
	NE=NW	DFQ 7450
	KSW1=0	DFQ 7460
	SW2=1	DFQ 7470
	KSW3=MCODE(23)	DFQ 7480
	KSW4=1	DFQ 7490
	KSW5=0	DFQ 7500
	GO TO 250	DFQ 7510
205	GO TO(206,207,490),KSW4	DFQ 7520
206	ZC=ZC+1	DFQ 7530
C	ENI 4 0 LIL 1 (2J-2)	DFQ 7540
	ZCODE(ZC)=MCODE(47)	DFQ 7550
	SW2=0.	DFQ 7560
	KSW4=2	DFQ 7570
	KSW5=2	DFQ 7580
	NT2=NR	DFQ 7590
	NL=NW	DFQ 7600
	NR=NW	DFQ 7610
	NE=NW	DFQ 7620
	GO TO 250	DFQ 7630
207	ZC=ZC+1	DFQ 7640
C	FDV (INTERVAL) V	DFQ 7650
	ZCODE(ZC)=MCODE(39)	DFQ 7660
	ZC=ZC+1	DFQ 7670
	ZCODE(ZC)=MCODE(4)+NV	DFQ 7680
	ZC=ZC+1	DFQ 7690
C	STA (INTERVAL) 2 W	DFQ 7700
	ZCODE(ZC)=MCODE(19)	DFQ 7710
	ZC=ZC+1	DFQ 7720
	ZCODE(ZC)=MCODE(3)+NW	DFQ 7730
	ZC=ZC+1	DFQ 7740
C	ENI 4 0 LIL 1 (2J-2)	DFQ 7750
	ZCODE(ZC)=MCODE(47)	DFQ 7760
	SW2=1	DFQ 7770
	NR=NT2	DFQ 7780
	NE=NT	DFQ 7790
	KSW3=MCODE(21)	DFQ 7800
	KSW4=3	DFQ 7810
	GO TO 250	DFQ 7820

```

C DFQ 7830
C DFQ 7840
C DFQ 7850
250 ZC=ZC+1 DFQ 7860
C 1) ENA 0 ENI 3 (0 OR 2) DFQ 7870
ZCODE(ZC)=MCODE(13)+KSW5 DFQ 7880
ZC=ZC+1 DFQ 7890
C 2) STA 2 NE STA 2 NE+1 DFQ 7900
ZCODE(ZC)=MCODE(14)+NE*100000001B DFQ 7910
ZC=ZC+1 DFQ 7920
IF(SW2)251,252 DFQ 7930
C 3) LDA (OR LAC) 3-NR DFQ 7940
251 ZCODE(ZC)=MCODE(15) DFQ 7950
ZC=ZC+1 DFQ 7960
ZCODE(ZC)=MCODE(1)+NR DFQ 7970
GO TO 253 DFQ 7980
252 ZCODE(ZC)=MCODE(16) DFQ 7990
ZC=ZC+1 DFQ 8000
ZCODE(ZC)=MCODE(1)+NR DFQ 8010
253 ZC=ZC+1 DFQ 8020
C 4) FMU 1 NL DFQ 8030
ZCODE(ZC)=MCODE(17) DFQ 8040
ZC=ZC+1 DFQ 8050
ZCODE(ZC)=MCODE(2)+NL+KSW1 DFQ 8060
ZC=ZC+1 DFQ 8070
C 8) RTJ (COM1 OR COM2 OR *+1) DFQ 8080
ZCODE(ZC)=KSW3 DFQ 8090
ZC=ZC+1 DFQ 8100
C 5) FAD 2 NE DFQ 8110
ZCODE(ZC)=MCODE(18) DFQ 8120
ZC=ZC+1 DFQ 8130
ZCODE(ZC)=MCODE(3)+NE DFQ 8140
ZC=ZC+1 DFQ 8150
C 6) STA 2 NE DFQ 8160
ZCODE(ZC)=MCODE(19) DFQ 8170
ZC=ZC+1 DFQ 8180
ZCODE(ZC)=MCODE(3)+NE DFQ 8190
ZC=ZC+1 DFQ 8200
C 7)INI 3 2 IJP 1 *+1 DFQ 8210
ZCODE(ZC)=KRAMDN(MCODE(20),ZCODE(ZC+1)) DFQ 8220
ZC=ZC+1 DFQ 8230
C 9) IJP 1 *-10 DFQ 8240
ZCODE(ZC)=KRAMDN(MCODE(24),ZCODE(ZC-10)) DFQ 8250
GO TO (2576,2157,490,145,1452,164,490,185,490,205),IND DFQ 8260
2576 ZC=ZC+1 DFQ 8270
GO TO 1576 DFQ 8280
2157 ZC=ZC+1

```

```

GO TO 157 DFQ 8290
C
C BOTH ARGUMENTS CONSTANT DFQ 8300
C 1) ENQ 2 0 QJP *+3 DFQ 8310
260 ZCODE(ZC)=KRAMDN(MCODE(25),ZCODE(ZC+3)) DFQ 8320
C 2) ENA 0 STA 2 NE DFQ 8330
ZC=ZC+1 DFQ 8340
ZCODE(ZC)=MCODE(26)+NE DFQ 8350
ZC=ZC+1 DFQ 8360
C 3) STA 2 NE+1 SLJ *+7 DFQ 8370
ZCODE(ZC)=KRAMDN(MCODE(27),ZCODE(ZC+7))+NE*LS8 DFQ 8380
C 4) LDA NL (REAL) DFQ 8390
ZC=ZC+1 DFQ 8400
ZCODE(ZC)=MCODE(28) DFQ 8410
ZC=ZC+1 DFQ 8420
ZCODE(ZC)=MCODE(4)+NL DFQ 8430
GO TO (118,128,138,148,158,168,168,168,168),IND DFQ 8440
C
C
490 IF(ZC.GT.999)699,491 DFQ 8450
491 IF(KSIN.GT.100)689,500 DFQ 8460
500 CONTINUE DFQ 8470
ZC=ZC+1 DFQ 8480
C SLJ EXIT DFQ 8490
ZCODE(ZC)=MCODE(51) DFQ 8500
RETURN DFQ 8510
689 CALL ERTST DFQ 8520
STOP DFQ 8530
699 CALL ERZCD DFQ 8540
STOP DFQ 8550
END DFQ 8560
IDENT DUMMYINT DFQ 8570
ENTRY DECODINT DFQ 8580
ENTRY STARTINT DFQ 8590
EXT Q1Q00550 DFQ 8600
EXT Q1Q01550 DFQ 8610
EXT Q1Q04550 DFQ 8620
EXT Q1Q02550 DFQ 8630
EXT Q1Q10550 DFQ 8640
EXT Q1Q00510 DFQ 8650
EXT Q1Q01510 DFQ 8660
EXT Q1Q02510 DFQ 8670
EXT Q1Q03550 DFQ 8680
EXT Q1Q03510 DFQ 8690
EXT Q1Q04510 DFQ 8700
EXT Q1Q05550 DFQ 8710
DFQ 8720
DFQ 8730
DFQ 8740

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	EXT	Q1QU5510	DFQ 8750	
	EXT	Q2Q07551	DFQ 8760	
	EXT	LOG5	DFQ 8770	
	EXT	EXP5	DFQ 8780	
	EXT	SIN5	DFQ 8790	
	EXT	COS5	DFQ 8800	
	EXT	ATAN5	DFQ 8810	
ERASABLE	BLOCK	973	DFQ 8820	
	COMMON	MASKSINT(60)	DFQ 8830	
CONSTANT	BLOCK	51	DFQ 8840	
	COMMON	C(51)	DFQ 8850	
ZLIST	BLOCK	1000	DFQ 8860	
	COMMON	ZCODE(1000)	DFQ 8870	
	ORGR	*	DFQ 8880	
DECODINT	SLJ	**	DFQ 8890	
+	SIU	EXIT,1	DFQ 8900	
	SIL	EXIT,2	DFQ 8910	
	SIU	EXIT+1,3	DFQ 8920	
	SIL	EXIT+1,4	DFQ 8930	
	SIU	EXIT+2,5	DFQ 8940	
	SIL	EXIT+2,6	DFQ 8950	
	LIL	DECUDINT,1	ADDRESS+1 OF CALL TO DECODE	DFQ 8960
	SIU	RETURN...,1	DFQ 8970	
	INI	1,1	DFQ 8980	
	LDA	0,1	ZRO(J) ENI 0	DFQ 8990
	ARS	24	DFQ 9000	
+	SAU	*+1	ADDRESS OF J	DFQ 9010
+	LDA	**	J TO A	DFQ 9020
	SAU	T	J TO UPPER OF T	DFQ 9030
	LIU	T,6	J TO I6	DFQ 9040
	INA	0,6	DFQ 9050	
	SAL	T	2J TO LOWER OF T	DFQ 9060
	INA	-2	DFQ 9070	
	SAL	T+5	DFQ 9080	
	LIL	T,2	2J TO I2	DFQ 9090
	ENA	0,6	DFQ 9100	
+	AJP,NZ	*+2	IS J = 0	DFQ 9110
	LDA	C+1	YES---	DFQ 9120
	STA	=SFACT	SET J-FACTORIAL = 1.	DFQ 9130
	SLJ	ZCODE	DFQ 9140	
	LDA	C,6	DFQ 9150	
	FMU	FACT	DFQ 9160	
	STA	FACT	DFQ 9170	
	SLJ	ZCODE	DFQ 9180	
EXIT	ENI	**,1	RESTORE	DFQ 9190
	ENI	**,2	INDEX	DFQ 9200

		REGISTERS		
ENI	**,3		DFQ 9210	
ENI	**,4		DFQ 9220	
ENI	**,5		DFQ 9230	
ENI	**,6		DFQ 9240	
RETURN..	SLJ	**	DFQ 9250	
STARTINT	SLJ	**	DFQ 9260	
+	SIU	EX2,1	DFQ 9270	
ENI		1,1	DFQ 9280	
LOOPSTAR	LDA	M1-1,1	DFQ 9290	
	STA	MASKSINT-1,1	DFQ 9300	
	ISK	60,1	DFQ 9310	
	SLJ	LOOPSTAR	DFQ 9320	
EX2	ENI	**,1	DFQ 9330	
	SLJ	STARTINT	DFQ 9340	
M1	DLDA	0,3	DFQ 9350	
M2	DLDA	0,1	DFQ 9360	
M3	DLDA	0,2	DFQ 9370	
M4	DLDA	0	DFQ 9380	
M5	DLDA	T+1	DFQ 9390	
M6	DLDA	FACT	DFQ 9400	
M7	BRTJ	(\$)LOG5,,*	DFQ 9410	
M8	BRTJ	(\$)EXP5,,*	DFQ 9420	
M9	BRTJ	(\$)COS5,,*	DFQ 9430	
M10	BRTJ	(\$)SIN5,,*	DFQ 9440	
M11	BRTJ	(\$)ATAN5,,*	DFQ 9450	
M12	BRTJ	(\$)Q1Q01510,,*	DFQ 9460	
M13	ENA	0	MULTIPLICATION LOOP	DFQ 9470
	ENI	0,3	SET I3 TO 0 OR 2	DFQ 9480
M14	STA	0,2	ZERO SUM	DFQ 9490
	STA	1,2		DFQ 9500
M15	BRTJ	(\$)Q1Q00550,,*	LDA 3 NR	DFQ 9510
M16	BRTJ	(\$)Q1Q01550,,*	(OR) LAC 3 NR	DFQ 9520
M17	BRTJ	(\$)Q1Q04550,,*	FMU 1 NL	DFQ 9530
M18	BRTJ	(\$)Q1Q02550,,*	FAD 2 NE	DFQ 9540
M19	BRTJ	(\$)Q1Q10550,,*	STA 2 NE	DFQ 9550
M20	INI	2,3	INI 3 2	DFQ 9560
	IJP	0,1	INI 1 -1 (UNLESS ZERO)	DFQ 9570
M21	RTJ	COM1		DFQ 9580
M22	RTJ	COM2		DFQ 9590
M23	ENI	0		DFQ 9600
M24	ENI	0		DFQ 9610
	IJP	0,1	IJP 1 *-6 (TO M3)	DFQ 9620
M25	ENQ	0,2		DFQ 9630
	QJP,ZR	0		DFQ 9640
M26	ENA	0		DFQ 9650
	STA	0,2		DFQ 9660

M27	STA	1,2		DFQ 9670
	SLJ	0		DFQ 9680
M28	BRTJ	(\$)Q1Q00510,,*	LDA (REAL)	DFQ 9690
M29	BRTJ	(\$)Q1Q00550,,*	LDA 2 (INTERVAL)	DFQ 9700
M30	LIU	T,1		DFQ 9710
	IJP	0,1		DFQ 9720
M31	BRTJ	(\$)Q1Q02510,,*	FAD (REAL)	DFQ 9730
M32	BRTJ	(\$)Q1Q03550,,*	FSB 2 (INTERVAL)	DFQ 9740
M33	BRTJ	(\$)Q1Q03510,,*	FSB (REAL)	DFQ 9750
M34	BRTJ	(\$)Q1Q04550,,*	FMU 2 (INTERVAL)	DFQ 9760
M35	BRTJ	(\$)Q1Q04510,,*	FMU (REAL)	DFQ 9770
M36	LIL	T,1		DFQ 9780
	IJP	0,1		DFQ 9790
M37	IJP	0,1		DFQ 9800
M38	SLJ	0		DFQ 9810
M39	BRTJ	(\$)Q1Q05550,,*	FDV (INTERVAL)	DFQ 9820
M40	BRTJ	(\$)Q1Q05510,,*	FDV (REAL)	DFQ 9830
M41	BRTJ	(\$)Q2Q07551,,*		DFQ 9840
M42	RTJ	COM3		DFQ 9850
	ZRO	0		DFQ 9860
M43	RTJ	COM4		DFQ 9870
	ZRO	0		DFQ 9880
M44	ENI	0,4		DFQ 9890
M45	LDA	0		DFQ 9900
	STA	T+1		DFQ 9910
M46	STA	T+2		DFQ 9920
M47	ENI	0,4		DFQ 9930
	LIL	T+5,1		DFQ 9940
M48	INI	2,1		DFQ 9950
M49	LIL	T,1		DFQ 9960
M50	ENI	0,4		DFQ 9970
	INI	-1,1		DFQ 9980
M51	SLJ	EXIT		DFQ 9990
M52	LDA	0,2		DFQ10000
	AJP,NZ	0		DFQ10010
M53	FSB	C+1		DFQ10020
	STA	0,2		DFQ10030
M54	LDA	0,2		DFQ10040
	FMU	0,2		DFQ10050
M55	STA	0,2		DFQ10060
M56	BRTJ	(\$)Q1Q04510,,*		DFQ10070
M57	BRTJ	(\$)Q1Q05510,,*		DFQ10080
M58	BRTJ	(\$)Q1Q01550,,*		DFQ10090
COM1	SLJ	**	PART OF MULTIPLY LOOP	DFQ10100
+	INI	1,4	FOR OBTAINING (J-K)/J	DFQ10110
	BRTJ	(\$)Q1Q04510,,*		DFQ10120

	DFMU	C,4	FMU (J-K)	DFQ10130
	BRTJ	(\$)Q1Q05510,,,*		DFQ10140
	DFDV	C,6	FDV (J)	DFQ10150
	SLJ	COM1		DFQ10160
COM2	SLJ	**	PART OF MULTIPLY LOOP	DFQ10170
+	INI	-1,5	FOR OBTAINING (C*(J-K)-K)/J	DFQ10180
COM21	BRTJ	(\$)Q1Q10550,,,*		DFQ10190
	DSTA	T+1	STA(T+1)	DFQ10200
COM22	BRTJ	(\$)Q1Q00510,,,*		DFQ10210
	DLDA	**	LDA (C)	DFQ10220
	BRTJ	(\$)Q1Q04510,,,*		DFQ10230
	DFMU	C,4	FMU (J-K)	DFQ10240
	BRTJ	(\$)Q1Q03510,,,*		DFQ10250
	DFSB	C,5	FSB (K)	DFQ10260
	BRTJ	(\$)Q1Q05510,,,*		DFQ10270
	DFDV	C,6	FDV (J)	DFQ10280
	BRTJ	(\$)Q1Q04550,,,*		DFQ10290
	DFMU	T+1	FMU (T+1)	DFQ10300
	INI	1,4		DFQ10310
	SLJ	COM2		DFQ10320
COM3	SLJ	**	INITIALIZATION FOR COM2	DFQ10330
+	LIU	COM3,5	ADDRESS OF CALL TO COM3	DFQ10340
	LDA	-1,5	C IN LOWER OF A	DFQ10350
	SAL	COM22+1		DFQ10360
	LIU	T,5	J (K+1 FOR K=J-1)	DFQ10370
	ENI	1,4	1 TO I4 (J-K FOR K=J-1)	DFQ10380
	INI	-1,1	2J-2 TO II	DFQ10390
	SLJ	COM3		DFQ10400
COM4	SLJ	**	REAL TO REAL	DFQ10410
+	LIU	COM4,5		DFQ10420
	LDA	-1,5		DFQ10430
	SAU	COM41		DFQ10440
	LDA	0,5		DFQ10450
	SAL	COM42+3		DFQ10460
COM41	LDA	**		DFQ10470
	STA	T+1	BASE TO TI	DFQ10480
	STA	T+2		DFQ10490
	INI	1,5		DFQ10500
COM42	BRTJ	(\$)Q2Q07551,,,*	EXPONENTIATE	DFQ10510
	SLJ	*+2		DFQ10520
	DLDA	T+1		DFQ10530
	DLDA	**	EXPONENT	DFQ10540
	SIU	COM4,5	SET UP EXIT	DFQ10550
	SLJ	COM4	EXIT	DFQ10560
T	BSS	6		DFQ10570
	ENTRY	ZPRINT		DFQ10580

ZPRINT	SLJ	**	DFQ10590
	CODAP		DFQ10600
+	SIU	6 ZEX	DFQ10610
	LIL	6 ZPRINT	DFQ10620
	SIL	6 ZEX	DFQ10630
	INI	6 1	DFQ10640
	LDQ	=077777	DFQ10650
	LDA	6 0	DFQ10660
	STL	T+3	ADDRESS OF OPR DFQ10670
	ARS	24	DFQ10680
	STL	T	ADDRESS OF ZCODE(I) DFQ10690
	LDA	6 1	DFQ10700
	STL	T+1	ADDRESS OF OPL DFQ10710
	ARS	24	DFQ10720
	STL	T+4	ADDRESS OF VR DFQ10730
	LDA	6 2	DFQ10740
	STL	T+5	ADDRESS OF OP DFQ10750
	ARS	24	DFQ10760
	STL	T+2	ADDRESS OF VL DFQ10770
	LDL	7 T	DFQ10780
	ALS	24	DFQ10790
	ENI	6 23	DFQ10800
	LDQ	=07777700000000	DFQ10810
+	MEQ	6 TABOP-1	DFQ10820
	SLJ	FOUND+1	DFQ10830
FOUND	LDQ	6 TABOP-1	DFQ10840
	SLJ	SORT	DFQ10850
	LDQ	=060606060	DFQ10860
SORT	STQ	7 T+5	DFQ10870
	LDA	7 T	DFQ10880
	LRS	15	DFQ10890
	QRS	33	DFQ10900
	STQ	7 T+4	DFQ10910
	LRS	9	DFQ10920
	QRS	39	DFQ10930
	STQ	7 T+3	DFQ10940
	LRS	15	DFQ10950
	QRS	33	DFQ10960
	STQ	7 T+2	DFQ10970
	STA	7 T+1	DFQ10980
ZEX	ENI	6 **	DFQ10990
	SLJ	**	DFQ11000
TABOP	RTJ	Q1Q00550	TABLE OF INT SUBROUTINES DFQ11010
-	SSU	2 42131B	AND THEIR NAMES DFQ11020
-	RTJ	Q1Q01550	DFQ11030
-	SSU	2 12331B	DFQ11040

RTJ		Q1Q04550	DFQ11050
MUF	4	46431B	DFQ11060
RTJ		Q1Q02550	DFQ11070
MUF	2	12431B	DFQ11080
RTJ		Q1Q10550	DFQ11090
62	6	32131B	DFQ11100
RTJ		Q1Q00510	DFQ11110
SSU	2	42151B	DFQ11120
RTJ		Q1Q01510	DFQ11130
SSU	2	12351B	DFQ11140
RTJ		Q1Q02510	DFQ11150
MUF	2	12451B	DFQ11160
RTJ		Q1Q03550	DFQ11170
MUF	6	22231B	DFQ11180
RTJ		Q1Q03510	DFQ11190
MUF	6	22251B	DFQ11200
RTJ		Q1Q04510	DFQ11210
MUF	4	46451B	DFQ11220
RTJ		Q1Q05550	DFQ11230
MUF	2	46531B	DFQ11240
RTJ		Q1Q05510	DFQ11250
MUF	2	46551B	DFQ11260
RTJ		Q2Q07551	DFQ11270
FSB	6	34651B	DFQ11280
RTJ		LOG5	DFQ11290
SSU	4	62726B	DFQ11300
RTJ		EXP5	DFQ11310
DVI	6	74726B	DFQ11320
RTJ		SIN5	DFQ11330
62	3	14526B	DFQ11340
RTJ		COS5	DFQ11350
QJP	4	66226B	DFQ11360
RTJ		ATAN5	DFQ11370
STQ	6	32145B	DFQ11380
RTJ		COM1	DFQ11390
QJP	4	64401B	DFQ11400
RTJ		COM2	DFQ11410
QJP	4	64402B	DFQ11420
RTJ		COM3	DFQ11430
QJP	4	64403B	DFQ11440
RTJ		COM4	DFQ11450
QJP	4	64404B	DFQ11460
COMPASS			DFQ11470
END			DFQ11480
SUBROUTINE COMPILE(NSYS,MAXNDER)			DFQ11490
EQUIVALENCE(SYMBOL,KYMBOL)			DFQ11500

```

TYPE INTEGER TNAME,DICTION DFQ11510
TYPE LOGICAL SW1,SW2 DFQ11520
COMMON/ERASABLE/MCODE(60),LEX,DICTION(30),KCOMP,LCOMOP(300), DFQ11530
1 LCOMVAR(300),LIBFUN(10),LOPT(50),LISTOP(50),LVAT(100),LILUB(50),DFQ11540
2 MTABLE(10),ITABLE(10),KTST DFQ11550
COMMON/CONSTANT/CONTAB(50),KCON DFQ11560
DATA(MASKHIGH=777777700000000B),(LSHIF8=100000000B),(MAXCP=300) DFQ11570
DATA(ML=7777777B) DFQ11580
DATA(LIBFUN=2060606000000000B,4060606000000000B,5460606000000000B,DFQ11590
1 616060600000000B,545460600000000B,434627260000000B, DFQ11600
2 256747260000000B,623145260000000B,234662260000000B, DFQ11610
3 216321450000000B) DFQ11620
C INITIALIZATION DFQ11630
KTST=KCOMP=LEX=MTCON=KEQ=0 DFQ11640
KCON=MAXNDER+1 DFQ11650
DO 1 N=1,KCON DFQ11660
1 CONTAB(N)=N-1 DFQ11670
PRINT 2 DFQ11680
2 FORMAT (23H0 FORMULAS COMPILED ARE //) DFQ11690
C READ LEFT SIDE OF FORMULA DFQ11700
10 CALL RDNUM(NAMEF) DFQ11710
NAMEF=NAMEF.AND.MASKHIGH DFQ11720
NPAR=NAMEF.AND.770000000000000B.OR.7R DFQ11730
IF(NPAR.EQ.1H)31,40 DFQ11740
C FORMULA IS PARAMETER DEFINITION DFQ11750
31 MTCON=MTCON+1 DFQ11760
MTABLE(MTCON)=NAMEF.OR.4R DFQ11770
CALL RDNUM(KYMBOL) DFQ11780
IF(KYMBOL.NE.1H=)1003,32 DFQ11790
32 CALL RDNUM(SYMBOL) DFQ11800
CALL ADCON(SYMBOL,ITABLE(MTCON)) DFQ11810
CALL RDNUM(SYMBOL) DFQ11820
IF(KYMBOL.NE.1H$)1003,10 DFQ11830
40 IF(NPAR.EQ.1H)45,41 DFQ11840
C SHORTHAND-SYMBOL-VARIABLE-ADD NAME TO LIST DFQ11850
41 LEX=LEX+1 DFQ11860
DICTION(LEX)=NAMEF/LSHIF8 DFQ11870
DICTION(LEX)=DICTION(LEX).AND.ML DFQ11880
GO TO 50 DFQ11890
C D-EQUATION DFQ11900
45 KEQ=KEQ+1 DFQ11910
50 CALL RDNUM(SYMBOL) DFQ11920
DFQ11930
DFQ11940
DFQ11950
DFQ11960

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C IF(KYMBOL.NE.1H=)1003,199 DFQ11970
C
C INITIALIZATION FOR COMPIILING FUNCTION DFQ11980
199 KVT=LBANK=SW2=LOPT(1)=LOPT(2)=0 DFQ11990
    LBANK=0 DFQ12000
    KOP=2 DFQ12010
    SW1=1 DFQ12020
    SW4=1. DFQ12030
    LISTOP(2)=1H+ DFQ12040
    LILUB(2)=1 DFQ12050
C
C OBTAIN NEXT SYMBOL DFQ12060
200 IF(SW4)2002,2001 DFQ12070
2001 SW4=1. DFQ12080
    KYMBOL=NEXTSYM DFQ12090
    GO TO 2003 DFQ12100
2002 CALL RDNUM(SYMBOL) DFQ12110
    CALL RDTYPE(LTYPE) DFQ12120
2003 IF(LTYPE)220,220,211 DFQ12130
C
C OPERATOR DFQ12140
220 IF(KYMBOL.EQ.1H())221,521 DFQ12150
221 IF(KYMBOL.EQ.1H())222,522 DFQ12160
522 IF(KYMBOL.EQ.1H$)226,526 DFQ12170
526 IF(KYMBOL.EQ.1H+.OR.KYMBOL.EQ.1H-)227,527 DFQ12180
527 IF(KYMBOL.EQ.1H*.OR.KYMBOL.EQ.1H/)228,528 DFQ12190
528 IF(KYMBOL.EQ.2H**)229,201 DFQ12200
C
C VARIABLE DFQ12210
201 KAR=KYMBOL.AND.700000000B DFQ12220
    IF(KAR.NE.0)225,2011 DFQ12230
2011 KAR=KYMBOL.AND.7700000000000000B.OR.60606060606060B DFQ12240
    IF(KAR.EQ.1HM)2012,202 DFQ12250
2012 CALL SEARCH(2,MTABLE,MTCON,IND,KYMBOL) DFQ12260
    IF(IND)2014,2013 DFQ12270
2013 CALL ERPAR DFQ12280
    STOP DFQ12290
2014 KYMBOL=ITABLE(IND) DFQ12300
202 KVT=KVT+1 DFQ12310
    LVAT(KVT)=KYMBOL DFQ12320
    SW2=1 DFQ12330
    GO TO 200 DFQ12340
C
C CONSTANT DFQ12350
211 CALL ADCON(SYMBOL,KYMBOL) DFQ12360
    GO TO 202 DFQ12370
DFQ12380
DFQ12390
DFQ12400
DFQ12410
DFQ12420

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C DFQ12430
C DFQ12440
C DFQ12450
C DFQ12460
C DFQ12470
C DFQ12480
C DFQ12490
C DFQ12500
C DFQ12510
C DFQ12520
C DFQ12530
C DFQ12540
C DFQ12550
C DFQ12560
C DFQ12570
C DFQ12580
C DFQ12590
C DFQ12600
C DFQ12610
C DFQ12620
C DFQ12630
C DFQ12640
C DFQ12650
C DFQ12660
C DFQ12670
C DFQ12680
C DFQ12690
C DFQ12700
C DFQ12710
C DFQ12720
C DFQ12730
C DFQ12740
C DFQ12750
C DFQ12760
C DFQ12770
C DFQ12780
C DFQ12790
C DFQ12800
C DFQ12810
C DFQ12820
C DFQ12830
C DFQ12840
C DFQ12850
C DFQ12860
C DFQ12870
C DFQ12880
C LEFT PAR. (
221 LBANK=LBANK+5 DFQ12430
      SW2=0 DFQ12440
      GO TO 200 DFQ12450
C RIGHT PAR.)
222 LBANK=LBANK-5 DFQ12460
      IF(LBANK)1003,200,200 DFQ12470
C END OPERATOR $
226 IF(LBANK.NE.0)1003,223 DFQ12480
223 SW1=LOPT(KOP-1) DFQ12490
      LCOP=0 DFQ12500
      GO TO 230 DFQ12510
C FUNCTION OPERATOR
225 LCOP=4+LBANK DFQ12520
2251 LUB=1 DFQ12530
      GO TO 230 DFQ12540
C + OR - OPERATOR
227 LCOP=1+LBANK DFQ12550
      IF(SW2)2281,2251 DFQ12560
C * OR / OPERATOR
228 LCOP=2+LBANK DFQ12570
2281 LUB=0 DFQ12580
      GO TO 230 DFQ12590
C ** OPERATOR
229 SW4=0. DFQ12600
      LCOP=3+LBANK DFQ12610
      CALL RDNUM(NEXTSYM) DFQ12620
      CALL RDTYPE(LTYPE) DFQ12630
      IF (LTYPE) 2292,2292,2282 DFQ12640
2282 SW5=1. DFQ12650
      GO TO 2281 DFQ12660
2292 KAR=NEXTSYM.AND.7700000000000000B .OR. 7R DFQ12670
      IF (KAR.EQ.1HM) 2282,2293 DFQ12680
2293 SW5=0. DFQ12690
      GO TO 230 DFQ12700
C EXPONENT IS NOT A CONSTANT - CODE A**B AS EXPF(B*LOGF(A)) DFQ12710
2291 LV2=LVAT(KVT)/LSHIF8 DFQ12720
      LV2=LV2.AND.77777777B DFQ12730
      KCOMP=KCOMP+1 DFQ12740

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```

NDEST=TNAME(DUMMY) DFQ12890
LCOMOP(KCOMP)=LIBFUN(6).OR.NDEST DFQ12900
LCOMVAR(KCOMP)=6060606000000000B.OR.LV2 DFQ12910
KOP=KOP+1 DFQ12920
LISTOP(KOP)=LIBFUN(7) DFQ12930
LOPT(KOP)=LCOP DFQ12940
LILUB(KOP)=1 DFQ12950
KYMBOl=LIBFUN(3) DFQ12960
LUB=0 DFQ12970
GO TO 250 DFQ12980
C DFQ12990
C COMPARE LEVEL OF CURRENT OP WITH THAT OF PRECEEDING DFQ13000
230 IF (LCOP .GT. LOPT(KOP) ) 240,550 DFQ13010
240 IF (SW4 .OR. SW5) 250,2291 DFQ13020
C PROCESS PRECEEDING OP. DFQ13030
550 SW1=LCOP.ORLOPT(KOP-1) DFQ13040
IF(SW1)231,551 DFQ13050
551 NDEST=NAMEF/LSHIF8 DFQ13060
NDEST=NDEST.AND.77777777B DFQ13070
GO TO 232 DFQ13080
231 NDEST=TNAME(DUMMY) DFQ13090
232 LOPDE=LISTOP(KOP).AND.MASKHIGH DFQ13100
KCOMP=KCOMP+1 DFQ13110
IF (KCOMP.GT.MAXCP)1005,552 DFQ13120
552 LCOMOP(KCOMP)=LOPDE.OR.NDEST DFQ13130
LV2=LVAT(KVT)/LSHIF8 DFQ13140
LV2=LV2.AND.77777777B DFQ13150
IF(LILUB(KOP))233,553 DFQ13160
C DFQ13170
C BINARY OPERATION DFQ13180
553 KVT=KVT-1 DFQ13190
LV1=LVAT(KVT).AND.MASKHIGH DFQ13200
GO TO 234 DFQ13210
C DFQ13220
C UNITARY OPERATION DFQ13230
C DFQ13240
233 LV1=6060606000000000B DFQ13250
234 LCOMVAR(KCOMP)=LV1.OR.LV2 DFQ13260
LVAT(KVT)=NDEST*LSHIF8 DFQ13270
KOP=KOP-1 DFQ13280
IF (SW1) 230,260 DFQ13290
C DFQ13300
C ADD CURRENT OP TO OP TABLE DFQ13310
250 KOP=KOP+1 DFQ13320
LISTOP(KOP)=KYMBOl DFQ13330
LOPT(KOP)=LCOP DFQ13340

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```

LILUB(KOP)=LUB DFQ13350
GO TO 200 DFQ13360
260 IF((LEX.GT.30).OR.(MTCON.GT.10))261,262 DFQ13370
261 CALL ERLEX DFQ13380
STOP DFQ13390
262 IF(KEQ.EQ.NSYS)263,10 DFQ13400
263 RETURN DFQ13410
C DFQ13420
C ERROR RETURNS DFQ13430
1003 PRINT 1021,NAMEF DFQ13440
1021 FORMAT(36H PARENTHESIS ERROR IN DEFINITION OF A4//)
RETURN DFQ13460
1005 CALL ERCOM DFQ13470
STOP DFQ13480
END DFQ13490
FUNCTION TNAME(DUMMY) DFQ13500
TYPE INTEGER TNAME DFQ13510
COMMON/ERASABLE/FIRST(972),K DFQ13520
K=K+1 DFQ13530
IF(K.GT.100)1,2 DFQ13540
1 CALL ERTST DFQ13550
STOP DFQ13560
2 TNAME=64*K+63B DFQ13570
RETURN DFQ13580
END DFQ13590
FUNCTION NAD(NAME,Y,D,Q,T,KS) DFQ13600
DIMENSION Y(1),D(1),Q(1),T(1) DFQ13610
COMMON/ERASABLE/MC(60),LEX,DICTION(30),MORE(881),KTST DFQ13620
COMMON/CONSTANT/C(50),NC DFQ13630
LB1=NAME.AND.77B DFQ13640
LBT=NAME/100B DFQ13650
LB2=LBT.AND.77B DFQ13660
LB3=LBT/100B DFQ13670
LB4=NAME/1000000B DFQ13680
LB3=LB3.AND.77B DFQ13690
LB4=LB4.AND.77B DFQ13700
IF(LB1.EQ.1RC)10,1 DFQ13710
1 IF(LB1.EQ.1RT)20,2 DFQ13720
2 IF(LB4.EQ.1RY)30,3 DFQ13730
3 IF(LB4.EQ.1RD)40,50 DFQ13740
C DFQ13750
C CONSTANT DFQ13760
10 NAD=KRAMDN(0,C(LBT)) DFQ13770
RETURN DFQ13780
C DFQ13790
C INTERMEDIATE STORAGE DFQ13800

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```

20 K=KS*(LBT-1)+1 DFQ13810
NAD=KRAMDN(0,T(K)) DFQ13820
RETURN DFQ13830
C DFQ13840
C Y DFQ13850
30 K=KRAMDN(0,Y(0)) DFQ13860
GO TO 41 DFQ13870
C DFQ13880
C D DFQ13890
40 K=KRAMDN(0,D(0)) DFQ13900
41 IF(LB2.EQ.60B)42,43 DFQ13910
42 NAD=K+(LB3-1)*KS+1 DFQ13920
RETURN DFQ13930
43 NAD=K+(LB3*10+LB2-1)*KS+1 DFQ13940
RETURN DFQ13950
C DFQ13960
C SHORTHAND-SYMBOL VARIABLE DFQ13970
50 CALL SEARCH(2,DICTION,LEX,IND,NAME) DFQ13980
K=KS*(IND-1)+1 DFQ13990
NAD=KRAMDN(0,Q(K)) DFQ14000
END DFQ14010
SUBROUTINE ERRORS DFQ14020
DIMENSION IFMT(5) DFQ14030
DATA(IFMT=8H(35HOLEN,8HGTH OF ,0,8HTABLE EX,8HCEEDED.)) DFQ14040
ENTRY ERCON DFQ14050
IFMT(3)=8HCONST. DFQ14060
10 PRINT IFMT DFQ14070
STOP DFQ14080
ENTRY ERLEX DFQ14090
IFMT(3)=8HLEXICON DFQ14100
GO TO 10 DFQ14110
ENTRY ERDIF DFQ14120
PRINT 11 DFQ14130
11 FORMAT(26HOUNDIFFERENTIABLE OP-CODE.) DFQ14140
STOP DFQ14150
ENTRY ERTST DFQ14160
IFMT(3)=8HT-STORE DFQ14170
GO TO 10 DFQ14180
ENTRY ERCOM DFQ14190
IFMT(3)=8HCOMPILE DFQ14200
GO TO 10 DFQ14210
ENTRY ERYCD DFQ14220
IFMT(3)=8HY-CODE DFQ14230
GO TO 10 DFQ14240
ENTRY ERZCD DFQ14250
IFMT(3)=8HZ-CODE DFQ14260

```

```

GO TO 10 DFQ14270
ENTRY ERPAR DFQ14280
PRINT 12 DFQ14290
12 FORMAT(22HO UNDEFINED PARAMETER.) DFQ14300
STOP DFQ14310
END DFQ14320
SUBROUTINE ADCON(CN,NCON) DFQ14330
COMMON/CONSTANT/C(50),KC DFQ14340
CALL SEARCH(2,C,KC,IND,CN) DFQ14350
IF(IND)5,1 DFQ14360
1 KC=KC+1 DFQ14370
IF(KC.GT.50)2,3 DFQ14380
2 CALL ERCON DFQ14390
STOP DFQ14400
3 C(KC)=CN DFQ14410
IND=KC DFQ14420
5 NCON=(IND*64+23B)*100000000B DFQ14430
RETURN DFQ14440
END DFQ14450
DFQ14460

ALLEN REITER'S SUBROUTINE SEARCH HAS BEEN REPLACED DFQ14470
BY THE LIBRARY SUBROUTINE OF THE SAME NAME DFQ14480
DFQ14490

SUBROUTINE RDNUM(ISIT) DFQ14500
TYPE INTEGER STAGE,COLCOUNT,COLMAX,CHARAC,CHARTYPE,OLDCHAR, DFQ14510
1 RDBYTE,WORD,TESDC,EXPONENT,DIGITS,ESIGN,SIGN DFQ14520
DIMENSION BUFFER(10),TYPETAB(4),DECISION(12),XPA(4),XPB(10), DFQ14530
1 XPC(10) DFQ14540
DATA(COLCOUNT=74),(COLMAX=73),(PRINTING=1.0),(MASK=77B), DFQ14550
1 (TYPETAB=111111111073000B,3555545555027007B,3555555555077000B, DFQ14560
1 675555555077000B),(DECISION=8H532==1=/,8H54TTTT/,8H6TTTTT/, DFQ14570
18H6////////,8H56V7VVV/,8H6VV7VVV/,8H9V8//7//,8H9V//8//,8H9VVVVVV/,DFQ14580
1 8H=XX==X=/,8HXXX==X=/,8H=XX==X=/),(XPA=1.0,1.0E100,1.0E200, DFQ14590
1 1.0E300),(XPB=1.0,1.0E10,1.0E20,1.0E30,1.0E40,1.0E50,1.0E60, DFQ14600
1 1.0E70,1.0E80,1.0E90),(XPC=1.0,10.0,100.0,1000.0,10000.0,1.0E5, DFQ14610
1 1.0E6,1.0E7,1.0E8,1.0E9) DFQ14620
EQUIVALENCE(X,I) DFQ14630
FLOATING=1.0 DFQ14640
GO TO 1 DFQ14650
ENTRY RDINT DFQ14660
FLOATING=0.0 DFQ14670
1 STAGE=1 DFQ14680
N=DIGITS=EXPONENT=WORD=TESDC=SIGN=ESIGN=0 DFQ14690
11 OLDCHAR=CHARAC DFQ14700
IF(COLCOUNT-COLMAX)3,6,2 DFQ14710
6 CHARAC=1R DFQ14720

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GO TO 7 DFQ14730
2 READ 500,(BUFFER(I),I=1,10) DFQ14740
500 FORMAT(10A8) DFQ14750
IF(PRINTING)4,5 DFQ14760
4 PRINT 501,(BUFFER(I),I=1,10) DFQ14770
501 FORMAT(X9A8,XA8) DFQ14780
5 COLCOUNT=1 DFQ14790
3 CHARAC=RDBYTE(BUFFER,COLCOUNT,8,64,MASK) DFQ14800
7 COLCOUNT=COLCOUNT+1 DFQ14810
CHARTYPE=RDBYTE(TYPETAB,CHARAC+1,16,8,7) DFQ14820
IF(CHARTYPE)130,131 DFQ14830
131 CHARTYPE=8 DFQ14840
130 STAGE=RDBYTE(DECISION(STAGE),CHARTYPE,8,64,MASK) DFQ14850
IF(STAGE-11)10,9,100 DFQ14860
9 STAGE=10 DFQ14870
10 GO TO (11,12,11,11,15,16,11,18,19,20),STAGE DFQ14880
12 IF(CHARAC-1R+)21,11 DFQ14890
21 SIGN=1 DFQ14900
GO TO 11 DFQ14910
15 IF OVERFLOW FAULT 22,22 DFQ14920
22 IF(CHARAC-10)24,25,25 DFQ14930
24 I=N+N DFQ14940
I=I+I+N DFQ14950
I=I+I+CHARAC DFQ14960
IF OVERFLOW FAULT 25,26 DFQ14970
26 N=I DFQ14980
GO TO 11 DFQ14990
25 DIGITS=DIGITS+1 DFQ15000
GO TO 11 DFQ15010
16 DIGITS=DIGITS-1 DFQ15020
GO TO 15 DFQ15030
18 IF((CHARAC-1R+)*(CHARAC-1R ))27,11 DFQ15040
27 ESIGN=1 DFQ15050
GO TO 11 DFQ15060
19 EXPONENT=EXPONENT*10+CHARAC DFQ15070
GO TO 11 DFQ15080
20 I=WORD.AND.770000000000000B DFQ15090
IF(I)11,28 DFQ15100
28 WORD=64*WORD DFQ15110
WORD=WORD.OR.CHARAC DFQ15120
GO TO 11 DFQ15130
C SCAN COMPLETE. PREPARE FOR EXIT DFQ15140
100 STAGE=STAGE+1-1R/ DFQ15150
GO TO (101,102,103,104,105,106,107),STAGE DFQ15160
101 I=COLCOUNT-1 DFQ15170
PRINT 502,I,CHARAC DFQ15180

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      GO TO 1                               DFQ15190
502 FORMAT(19H INPUT ERROR COLUMN I3,11H CHARACTER 02)   DFQ15200
103 COLCOUNT=COLCOUNT-1                  DFQ15210
      CHARAC=OLDCHAR                      DFQ15220
102 ISIT=CHARAC*1000000000000000B        DFQ15230
      ISIT=7R          .OR.ISIT           DFQ15240
114 RETURN                                DFQ15250
105 COLCOUNT=COLCOUNT-1                  DFQ15260
104 DIGITS=DIGITS+(1-ESIGN-ESIGN)*EXPONENT    DFQ15270
      TESDC=1                           DFQ15280
      N=N*(1-SIGN-SIGN)                 DFQ15290
108 IF(FLOATING)124,109                  DFQ15300
109 ISIT=N                               DFQ15310
      IF(DIGITS)126,114,111             DFQ15320
111 IFOVERFLOW FAULT 112,112            DFQ15330
112 DO 120 I=1,DIGITS                  DFQ15340
      N=ISIT+ISIT                      DFQ15350
      N=N+N+ISIT                      DFQ15360
120 ISIT=N+N                         DFQ15370
      IF OVERFLOW FAULT 113,114         DFQ15380
113 PRINT 503                            DFQ15390
503 FORMAT(18H INTEGER TOO LARGE)       DFQ15400
      ISIT=37777777777777777B          DFQ15410
      GO TO 114                          DFQ15420
126 DIGITS=-DIGITS                     DFQ15430
      DO 125 I=1,DIGITS               DFQ15440
125 ISIT=ISIT/10                       DFQ15450
      GO TO 114                          DFQ15460
124 X=N                                 DFQ15470
      K=XABSF(DIGITS)                 DFQ15480
      J1=K/100                          DFQ15490
      K=K-100*J1                      DFQ15500
      J2=K/10                          DFQ15510
      K=K-J2*10                      DFQ15520
      Y=XPA(J1+1)*XPB(J2+1)*XPC(K+1)  DFQ15530
      IF(DIGITS)115,116,117            DFQ15540
115 X=X/Y                             DFQ15550
116 ISIT=I                            DFQ15560
      GO TO 114                          DFQ15570
117 X=X*Y                            DFQ15580
      GO TO 116                          DFQ15590
107 COLCOUNT=COLCOUNT-1                DFQ15600
106 TESDC=-1                          DFQ15610
      ISIT=WORD                         DFQ15620
      I=WORD.AND.7700000000000000B     DFQ15630
      IF(I)114,132                      DFQ15640

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```

132 WORD=WORD*64 DFQ15650
WORD=WORD.OR.1R DFQ15660
GO TO 106 DFQ15670
ENTRY RDTYPE DFQ15680
ISIT=TESDC DFQ15690
GO TO 114 DFQ15700
ENTRY RDPRINT DFQ15710
PRINTING=ISIT DFQ15720
GO TO 114 DFQ15730
ENTRY RDMODE DFQ15740
GO TO (201,202),ISIT DFQ15750
201 DECISION(10)=DECISION(11) DFQ15760
GO TO 114 DFQ15770
202 DECISION(10)=DECISION(12) DFQ15780
GO TO 114 DFQ15790
END DFQ15800
FUNCTION RDBYTE(I,J,K,KK,MASK) DFQ15810
DIMENSION I(10) DFQ15820
N=(J-1)/K DFQ15830
M=K+K*N-J DFQ15840
II=I(N+1) DFQ15850
IF(M)1,1,2 DFQ15860
2 NN=1 DFQ15870
DO 3 N=1,M DFQ15880
3 NN=NN*KK DFQ15890
II=II/NN DFQ15900
1 RDBYTE=II.AND.MASK DFQ15910
END DFQ15920
IDENT KRAM DFQ15930
CODAP DFQ15940
ENTRY KRAMDN DFQ15950
KRAMDN SLJ ** DFQ15960
+ SIU 6 EXIT DFQ15970
LIL 6 KRAMDN DFQ15980
SIL 6 EXIT DFQ15990
INI 6 1 DFQ16000
LDA 6 0 DFQ16010
STA =SSAV DFQ16020
LIU 6 SAV DFQ16030
SCL =0-77777 DFQ16040
ADD 6 0 DFQ16050
EXIT ENI 6 ** DFQ16060
SLJ ** DFQ16070
ENTRY KRAMUP DFQ16080
KRAMUP SLJ ** DFQ16090
+ SIU 6 EXIT DFQ16100

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LIL	6	KRAMUP	DFQ16110
SIL	6	EXIT	DFQ16120
INI	6	1	DFQ16130
LDA	6	0	DFQ16140
STA		SAV	DFQ16150
LIU	6	SAV	DFQ16160
SCL		=0-77777	DFQ16170
ALS		24	DFQ16180
ADD	6	0	DFQ16190
SLJ		EXIT	DFQ16200
COMPASS			DFQ16210
END			DFQ16220
IDENT		INTERVAL	INTERVAL ARITHMETIC PACKAGE DFQ16230
EXT		LOG5	DFQ16240
EXT		EXP5	DFQ16250
EXT		SPOPSADD	DFQ16260
EXT		SPOPSMUL	DFQ16270
EXT		SPOPSDIV	DFQ16280
EXT		ERRORINT	DFQ16290
DICT.	OCT	0	DFQ16300
	BCD	1, INTERVAL	DFQ16310
A	OCT	0	DFQ16320
	OCT	0	DFQ16330
B	OCT	0	DFQ16340
	OCT	0	DFQ16350
TEMP	BSS	4	DFQ16360
	ENTRY	Q1Q00530	DFQ16370
Q1Q00530	BSS	0	DFQ16380
	ENTRY	Q1Q00550	LOAD ACC WITH INTERVAL DFQ16390
Q1Q00550	SLJ	**	DFQ16400
+	RTJ	IN1	DFQ16410
+	LDA	A,7	DFQ16420
	STA	=SEL	DFQ16430
	LDA	A+1,7	DFQ16440
Q005	STA	=SER	DFQ16450
	SLJ	EXIT	DFQ16460
	ENTRY	Q1Q01530	DFQ16470
Q1Q01530	BSS	0	DFQ16480
	ENTRY	Q1Q01550	LOAD NEGATIVE WITH INTERVAL DFQ16490,
Q1Q01550	SLJ	**	DFQ16500
+	RTJ	IN1	DFQ16510
+	LAC	A+1,7	DFQ16520
	STA	EL	DFQ16530
	LAC	A,7	DFQ16540
	SLJ	Q005	DFQ16550
	ENTRY	Q1Q00500	LDA WITH INTEGER DFQ16560

Q1Q00500	SLJ	**	DFQ16570
+	RTJ	IN1	DFQ16580
+	LDA	A,7	DFQ16590
Q054	RTJ	FLOAT	DFQ16600
Q05	STA	=SEL	DFQ16610
	SLJ	Q005	DFQ16620
	ENTRY	Q1Q01500	LAC WTH INTEGER
Q1Q01500	SLJ	**	DFQ16630
+	RTJ	IN1	DFQ16640
+	LAC	A,7	DFQ16650
	SLJ	Q054	DFQ16660
	ENTRY	Q1Q00510	LDA WITH REAL
Q1Q00510	SLJ	**	DFQ16680
+	RTJ	IN1	DFQ16690
+	LDA	A,7	DFQ16700
	SLJ	Q05	DFQ16710
	ENTRY	Q1Q01510	LAC WITH REAL
Q1Q01510	SLJ	**	DFQ16730
+	RTJ	IN1	DFQ16740
+	LAC	A,7	DFQ16750
	SLJ	Q05	DFQ16760
	ENTRY	Q1Q02500	ADD INTEGER
Q1Q02500	SLJ	**	DFQ16780
+	RTJ	IN1	DFQ16790
+	LDA	A,7	DFQ16800
ADINT	RTJ	FLOAT	DFQ16810
ADREAL	STA	=SSAVA	DFQ16820
+	LDQ	EL	DFQ16830
	RTJ	SPOPSADD	DFQ16840
	STQ	EL	DFQ16850
	LDA	SSAVA	DFQ16860
+	LDQ	ER	DFQ16870
	RTJ	SPOPSADD	DFQ16880
	SLJ	Q005	DFQ16890
	ENTRY	Q1Q03500	SUBTRACT INTEGER
Q1Q03500	SLJ	**	DFQ16910
+	RTJ	IN1	DFQ16920
+	LAC	A,7	DFQ16930
	SLJ	ADINT	DFQ16940
	ENTRY	Q1Q02510	ADD REAL
Q1Q02510	SLJ	**	DFQ16960
+	RTJ	IN1	DFQ16970
+	LDA	A,7	DFQ16980
	SLJ	ADREAL	DFQ16990
	ENTRY	Q1Q03510	SUBTRACT REAL
Q1Q03510	SLJ	**	DFQ17000

+	RTJ	IN1	DFQ17030
+	LAC	A,7	DFQ17040
	SLJ	ADREAL	DFQ17050
	ENTRY	Q1Q02530	DFQ17060
Q1Q02530	BSS	0	DFQ17070
	ENTRY	Q1Q02550	DFQ17080
Q1Q02550	SLJ	**	DFQ17090
+	RTJ	IN1	DFQ17100
AD55	LDA	A,7	DFQ17110
+	LDQ	EL	DFQ17120
	RTJ	SPOPSADD	DFQ17130
	STQ	EL	DFQ17140
	LDA	A+1,7	DFQ17150
AD5	LDQ	ER	DFQ17160
	RTJ	SPOPSADD	DFQ17170
	SLJ	Q005	DFQ17180
	ENTRY	Q1Q03530	DFQ17190
Q1Q03530	BSS	0	DFQ17200
	ENTRY	Q1Q03550	SUBTRACT INTERVAL
Q1Q03550	SLJ	**	DFQ17210
+	RTJ	IN1	DFQ17220
SUB55	LAC	A+1,7	DFQ17230
+	LDQ	EL	DFQ17240
	RTJ	SPOPSADD	DFQ17250
	STQ	EL	DFQ17260
	LAC	A,7	DFQ17270
	SLJ	AD5	DFQ17280
	ENTRY	Q1Q04500	DFQ17290
Q1Q04500	SLJ	**	DFQ17300
+	RTJ	IN1	DFQ17310
+	LDA	A,7	DFQ17320
	RTJ	FLOAT	DFQ17330
Q0315	STA	=SDL	DFQ17340
	STA	=SDR	DFQ17350
MULT	LDA	DL	DFQ17360
+	LDQ	EL	DFQ17370
	RTJ	SPOPSMUL	DFQ17380
	STA	=STMAY	DFQ17390
	STQ	=STMIN	DFQ17400
	LDA	DL	DFQ17410
+	LDQ	ER	DFQ17420
	RTJ	SPOPSMUL	DFQ17430
	RTJ	MAXMIN	DFQ17440
+	LDA	DR	DFQ17450
+	LDQ	EL	DFQ17460
	RTJ	SPOPSMUL	DFQ17470
			DFQ17480

	RTJ	MAXMIN	DFQ17490
+	LDA	DR	DFQ17500
+	LDQ	ER	DFQ17510
	RTJ	SPOPSMUL	DFQ17520
	RTJ	MAXMIN	DFQ17530
+	LDA	TMIN	DFQ17540
	STA	EL	DFQ17550
	LDA	TMAX	DFQ17560
	SLJ	Q005	DFQ17570
	ENTRY	Q1Q04510	MULTIPLY BY REAL
Q1Q04510	SLJ	**	DFQ17590
+	RTJ	IN1	DFQ17600
+	LDA	A,7	DFQ17610
	SLJ	Q0315	DFQ17620
	ENTRY	Q1Q04530	MULTIPLY BY INTERVAL
Q1Q04530	BSS	0	DFQ17640
	ENTRY	Q1Q04550	MULTIPLY BY INTERVAL
Q1Q04550	SLJ	**	DFQ17650
+	RTJ	IN1	DFQ17660
Q0455	LDA	A,7	DFQ17670
	STA	=SDL	DFQ17680
	LDA	A+1,7	DFQ17690
	STA	=SDR	DFQ17700
	SLJ	MULT	DFQ17710
	ENTRY	Q1Q05530	DFQ17720
Q1Q05530	BSS	0	DFQ17730
	ENTRY	Q1Q05550	DIVIDE BY INTERVAL
Q1Q05550	SLJ	**	DFQ17740
+	RTJ	IN1	DFQ17750
Q555	LDA	A,7	DFQ17760
	AJP,ZR	ERRDIV	DFQ17770
	AJP,PL	Q5551	DFQ17780
	LDA	A+1,7	DFQ17790
	AJP,ZR	ERRDIV	DFQ17800
	AJP,PL	ERRDIV	DFQ17810
Q5551	LDA	F1	DFQ17820
+	LDQ	A+1,7	DFQ17830
	RTJ	SPOPSDIV	DFQ17840
	STQ	DL	DFQ17850
	LDA	F1	DFQ17860
+	LDQ	A,7	DFQ17870
	RTJ	SPOPSDIV	DFQ17880
	STA	DR	DFQ17890
	SLJ	MULT	DFQ17900
	ENTRY	Q1Q05500	DIVIDE BY INTEGER
Q1Q05500	SLJ	**	DFQ17910
			DFQ17920
			DFQ17930
			DFQ17940

+	RTJ	IN1	DFQ17950
+	LDA	A,7	DFQ17960
	RTJ	FLOAT	DFQ17970
Q055	STA	DL	DFQ17980
	AJP,ZR	ERRDIV	DFQ17990
	LDA	F1	DFQ18000
+	LDQ	DL	DFQ18010
	RTJ	SPOPSDIV	DFQ18020
	STQ	DL	DFQ18030
	STA	DR	DFQ18040
	SLJ	MULT	DFQ18050
	ENTRY	Q1Q05510	DIVIDE BY REAL
Q1Q05510	SLJ	**	DFQ18060
+	RTJ	IN1	DFQ18070
+	LDA	A,7	DFQ18080
	SLJ	Q055	DFQ18090
ERRDIV	BRTJ	(\$)ERRORINT,,*	DFQ18100
+	SLJ	EXIT	DFQ18110
	ENTRY	Q1Q10050	STORE INTEGER
Q1Q10050	SLJ	**	DFQ18120
+	RTJ	IN1	DFQ18130
+	RTJ	FLOAT	DFQ18140
Q100	STA	A,7	DFQ18150
	STA	A+1,7	DFQ18160
	STA	=SEL	DFQ18170
	STA	=SER	DFQ18180
	SLJ	EXIT	DFQ18190
	ENTRY	Q1Q10150	STORE REAL
Q1Q10150	SLJ	**	DFQ18200
+	RTJ	IN1	DFQ18210
+	SLJ	Q100	DFQ18220
	ENTRY	Q1Q10550	STORE INTERVAL
Q1Q10550	SLJ	**	DFQ18230
+	RTJ	IN1	DFQ18240
+	LDA	EL	DFQ18250
	STA	A,7	DFQ18260
	LDQ	ER	DFQ18270
	STQ	A+1,7	DFQ18280
	SLJ	EXIT	DFQ18290
	ENTRY	Q1Q10510	STORE INTERVAL IN REAL
Q1Q10510	SLJ	**	-----TAKES AVERAGE
+	RTJ	IN1	DFQ18340
+	LDA	EL	DFQ18350
	FAD	ER	DFQ18360
	FDV	=020024000000000000	DFQ18370
	STA	A,7	DFQ18380
			DFQ18390
			DFQ18400

	SLJ	EXIT	DFQ18410	
	ENTRY	Q1Q10500	DFQ18420	
Q1Q10500	SLJ	**	DFQ18430	
+	RTJ	IN1	DFQ18440	
+	LDA	EL	DFQ18450	
	FAD	ER	DFQ18460	
	FDV	=0200240000000000	DFQ18470	
	RTJ	FIX	DFQ18480	
+	STA	A,7	DFQ18490	
	SLJ	EXIT	DFQ18500	
	ENTRY	Q0Q06500	COMPLEMENT ACC	DFQ18510
Q0Q06500	SLJ	**	DFQ18520	
+	LAC	EL	DFQ18530	
	LQC	ER	DFQ18540	
	STQ	EL	DFQ18550	
	STA	ER	DFQ18560	
	SLJ	Q0Q06500	DFQ18570	
	ENTRY	Q2Q07055,Q2Q07155,Q2Q07555	INTERVAL EXPONENT - TREAT DFQ18580	
	BSS	0	SET OF POWERS DFQ18590	
Q2Q07155	BSS	0	DFQ18600	
Q2Q07555	SLJ	**	DFQ18610	
+	RTJ	IN2	DFQ18620	
+	LDA	A+1,7	DFQ18630	
	STA	TEMP+3	DFQ18640	
Q071	LDA	A,7	DFQ18650	
	STA	TEMP+2	EXPOENT TO TEMP+2 DFQ18660	
	LDA	B,7	DFQ18670	
	AJP,ZR	ERREXP	DFQ18680	
	AJP,MI	ERREXP	DFQ18690	
	STA	TEMP	DFQ18700	
	LDA	B+1,7	DFQ18710	
	STA	TEMP+1	DFQ18720	
Q072	BRTJ	(\$)LOG5,,*	DFQ18730	
	SLJ	*+2	DFQ18740	
	01	DICT.	DFQ18750	
	00	(\$)TEMP	DFQ18760	
+	BRTJ	(\$)Q1Q04550,,*	FMU(TEMP) DFQ18770	
	DLDA	TEMP+2	TEMP*EXPONENT TO ACC DFQ18780	
+	BRTJ	(\$)Q1Q10550,,*	DFQ18790	
	DSTA	TEMP	TEMP=EXPONENT * LOG(BASE) DFQ18800	
	BRTJ	(\$)EXP5,,*	DFQ18810	
	SLJ	*+2	DFQ18820	
	01	DICT.	DFQ18830	
+	00	(\$)TEMP	DFQ18840	
+	SLJ	EX2	DFQ18850	
ERREXP	BRTJ	(\$)ERRORINT,,*	DFQ18860	

+	SLJ	EX2	DFQ18870
	ENTRY	Q2Q07115,Q2Q07515,Q2Q07015	DFQ18880
Q2Q07015	BSS	0	DFQ18890
Q2Q07115	BSS	0	DFQ18900
Q2Q07515	SLJ	**	REAL TO INTERVAL POWER DFQ18910
+	RTJ	IN2	DFQ18920
+	LDA	B,7	DFQ18930
RTIP	AJP,ZR	ERREXP	DFQ18940
	AJP,MI	ERREXP	DFQ18950
	STA	TEMP	DFQ18960
	STA	TEMP+1	DFQ18970
	LDQ	A,7	DFQ18980
	STQ	TEMP+2	DFQ18990
	LDQ	A+1,7	DFQ19000
	STQ	TEMP+3	DFQ19010
	SLJ	Q072	DFQ19020
	ENTRY	Q2Q07005,Q2Q07105,Q2Q07505	DFQ19030
Q2Q07005	BSS	0	DFQ19040
Q2Q07105	BSS	0	DFQ19050
Q2Q07505	SLJ	**	INTEGER TO INTERVAL POWER DFQ19060
+	RTJ	IN2	DFQ19070
+	LDA	B,7	DFQ19080
	RTJ	FLOAT	DFQ19090
	SLJ	RTIP	DFQ19100
	ENTRY	Q2Q07050,Q2Q07150,Q2Q07550	INTEGER EXPONENTS DFQ19110
Q2Q07050	BSS	0	-TREATED AS INTERVAL PRODUCTS DFQ19120
Q2Q07150	BSS	0	TAKEN N TIMES DFQ19130
Q2Q07550	SLJ	**	DFQ19140
+	RTJ	IN2	DFQ19150
+	LDA	A,7	J=EXPONENT DFQ19160
	RTJ	TESTEXP	DFQ19170
REMULTI	LDQ	B,7	DFQ19180
	STQ	TEMP	DFQ19190
	LDQ	B+1,7	DFQ19200
	STQ	TEMP+1	Y=BASE DFQ19210
	LDQ	F1	DFQ19220
	STQ	TEMP+2	DFQ19230
	STQ	TEMP+3	P=1 DFQ19240
LOOP	ENQ	0	DFQ19250
	LRS	1	DFQ19260
	STA	=SJ	J=J/2 DFQ19270
	QJP,ZR	PASS	SKIP IF LOW-ORDER BIT=0 DFQ19280
	BRTJ	(\\$)Q1Q00550,,*	DFQ19290
	DLDA	TEMP	LDA (TEMP) DFQ19300
	BRTJ	(\\$)Q1Q04550,,*	DFQ19310
	DLDA	TEMP+2	FMU(TEMP+2) DFQ19320

PASS	BRTJ	(\$)Q1Q1055U,,*	STA(TEMP+2)	DFQ19330
	DSTA	TEMP+2	P=P*Y	DFQ19340
	BRTJ	(\$)Q1Q00550,,*	LDA(TEMP)	DFQ19350
	DLDA	TEMP		DFQ19360
	BRTJ	(\$)Q1Q04550,,*	FMU(TEMP)	DFQ19370
	DLDA	TEMP		DFQ19380
	BRTJ	(\$)Q1Q10550,,*	STA(TEMP)	DFQ19390
	DSTA	TEMP	Y=Y*Y	DFQ19400
	LDA	J		DFQ19410
ENDEXP	AJP,NZ	LOOP	END IF J=0	DFQ19420
	LDQ	SEXp		DFQ19430
	QJP,PL	EXPUS		DFQ19440
	BRTJ	(\$)Q1Q00510,,*		DFQ19450
	DLDA	F1	LDA 1.	DFQ19460
	BRTJ	(\$)Q1Q05550,,*		DFQ19470
	DLDA	TEMP+2	FDV B	DFQ19480
	SLJ	EX2		DFQ19490
EXPOS	BRTJ	(\$)Q1Q00550,,*	LDA B	DFQ19500
	DLDA	TEMP+2		DFQ19510
	SLJ	EX2	EXIT	DFQ19520
TESTEXP	SLJ	**	CHECK FOR NEGATIVE EXPONENT	DFQ19530
	AJP,PL	POSEXP		DFQ19540
	ENQ	-1	-1 FOR NEGATIVE EXPONENT	DFQ19550
	SCM	ALSEV	COMPLEMENT A	DFQ19560
	STQ	=SSEXP		DFQ19570
	SLJ	TESTEXP		DFQ19580
POSEXP	ENQ	1	+1 FOR POSITIVE EXPONENT	DFQ19590
	SLJ	*-1		DFQ19600
	ENTRY	Q2Q07553		DFQ19610
Q2Q07553	BSS	0		DFQ19620
	ENTRY	Q2Q07051,Q2Q07151,Q2Q07551	REAL EXPONENT - SET OF	DFQ19630
Q2Q07051	BSS	0		DFQ19640
Q2Q07151	BSS	0		DFQ19650
Q2Q07551	SLJ	**		DFQ19660
+	RTJ	IN2		DFQ19670
+	LDA	A,7		DFQ19680
+	RTJ	FIX	FIX EXPONENT	DFQ19690
+	STA	=SK1	TEST FOR INTEGER	DFQ19700
+	RTJ	FLOAT		DFQ19710
+	FSB	A,7		DFQ19720
	AJP,ZR	WHOLE	EXACT INTEGER IF A=0	DFQ19730
	LDA	A,7		DFQ19740
	STA	TEMP+3		DFQ19750
	SLJ	Q071		DFQ19760
WHOLE	LDA	K1		DFQ19770
	RTJ	TESTEXP		DFQ19780

	LDQ	B,7	DFQ19790
	QJP,PL	REMULTI	DFQ19800
	LDQ	B+1,7	ALGORITHM IS SAME AS INTEGER EXPDFQ19810
	QJP,MI	REMULTI	DFQ19820
	STA	K1	DFQ19830
	ENQ	1	DFQ19840
	LDL	K1	TEST FOR EVEN OR ODD DFQ19850
	AJP,ZR	EVEN	DFQ19860
	LDA	K1	DFQ19870
	LDQ	B,7	ODD EXPONENT DFQ19880
	RTJ	REPEAT1	DFQ19890
+	STQ	TEMP+1	DFQ19900
	SLJ	REPEAT2	DFQ19910
+	LDQ	TEMP+1	LOWER RESULT DFQ19920
	STQ	TEMP+2	DFQ19930
	LDQ	B+1,7	DFQ19940
UPPER	LDA	K1	OBTAIN RIGHT ENDPOINT DFQ19950
	RTJ	REPEAT1	DFQ19960
+	STA	TEMP+1	UPPER RESULT DFQ19970
	SLJ	REPEAT2	DFQ19980
+	LDQ	TEMP+1	DFQ19990
	STQ	TEMP+3	DFQ20000
	SLJ	ENDEXP	DFQ20010
EVEN	ENQ	0	EVEN EXPONENT DFQ20020
	STQ	TEMP+2	SET LEFT END-POINT TO ZERO DFQ20030
	LAC	B,7	DFQ20040
	LDQ	B+1,7	FIND BIGGER(IN ABSOLUTE DFQ20050
	STQ	TEMP+3	VALUE) OF THE TWO END-POINTS DFQ20060
+	THS	TEMP+3	DFQ20070
	STA	TEMP+3	DFQ20080
	LDQ	TEMP+3	DFQ20090
	SLJ	UPPER	DFQ20100
REPEAT1	SLJ	**	DFQ20110
	STQ	TEMP	Y=BASE DFQ20120
	LDQ	F1	DFQ20130
	STQ	TEMP+1	DFQ20140
LOOPLOOP	ENQ	0	DFQ20150
	LRS	1	J=J/2 DFQ20160
	STA	J	DFQ20170
	QJP,ZR	REPEAT2	SKIP MULTIPLICATION OF P BY Y DFQ20180
	LDA	TEMP	IF LOW-ORDER BIT OF J IS ZERO DFQ20190
	LDQ	TEMP+1	DFQ20200
	RTJ	SPOPSMUL	DFQ20210
+	SLJ	REPEAT1	DFQ20220
REPEAT2	LDA	TEMP	EXIT TO STA/STQ DFQ20230
	LDQ	TEMP	DFQ20240

	RTJ	SPOPSMUL	Y=Y*Y	DFQ20250
	STA	TEMP		DFQ20260
	LDA	J		DFQ20270
	AJP,NZ	LOOPLOOP	END IF J=0	DFQ20280
	LDA	REPEAT1	SET UP EXIT	DFQ20290
	ARS	24		DFQ20300
	INA	1		DFQ20310
	SAU	*+1		DFQ20320
+ IN1	SLJ	**	EXIT	DFQ20330
+ IN1	SLJ	**	INITIALIZATION FOR Q1Q	DFQ20340
	SIU	END1,1		DFQ20350
	LIU	IN1,1		DFQ20360
	INI	-2,1		DFQ20370
	STA	=SSAVA		DFQ20380
	RAO	0,1		DFQ20390
	SIU	*+1,1	A44. OF CALL TO IN1	DFQ20400
	SIU	EXIT,1	SET UP EXIT	DFQ20410
	LIL	**,1		DFQ20420
	INI	-1,1		DFQ20430
	LDA	0,1		DFQ20440
	STA	A		DFQ20450
	INA	1		DFQ20460
	STA	A+1		DFQ20470
	LDA	SSAVA	RESTORE A	DFQ20480
END1	ENI	**,1		DFQ20490
	SLJ	IN1	EXIT	DFQ20500
IN2	SLJ	**	INITIALIZATION FOR Q2Q	DFQ20510
	SIU	END2,1		DFQ20520
	LIU	IN2,1	ADD.+1 OF CALL TO IN2	DFQ20530
	INI	-2,1		DFQ20540
	SIU	*+1,1		DFQ20550
	STA	SSAVA	SAVE A	DFQ20560
+ END2	LIL	**,1		DFQ20570
	SIU	EX2,1		DFQ20580
	INI	1,1		DFQ20590
	LDA	0,1	CALL TO Q2Q	DFQ20600
	STA	B		DFQ20610
	INA	1		DFQ20620
	STA	B+1		DFQ20630
	INI	1,1		DFQ20640
	LDA	0,1		DFQ20650
	STA	A		DFQ20660
	INA	1		DFQ20670
	STA	A+1		DFQ20680
	LDA	SSAVA	RESTORE A	DFQ20690
	ENI	**,1	RESTORE I1	DFQ20700

EXIT	SLJ	IN2		DFQ20710
EX2	SLJ	**	EXIT FOR Q1Q'S	DFQ20720
FIX	SLJ	**	EXIT FOR Q2Q'S	DFQ20730
	AJP,MI	FIXNEG	EXIT FOR NEGATIVE	DFQ20740
	FAD	HEXP	POSITION COEFFICIENT IN A	DFQ20750
	SCL	HEXP	CLEAR HIGH BITS	DFQ20760
	SLJ	FIX		DFQ20770
FIXNEG	FSB	HEXP		DFQ20780
	SST	HEXP		DFQ20790
	SLJ	FIX		DFQ20800
HEXP	OCT	2044400000000000		DFQ20810
FLOAT	SLJ	**	FLOAT FIXED-POINT NUMBER	DFQ20820
	AJP,MI	FLN		DFQ20830
	SST	MONE	PUT IN EXPONENT	DFQ20840
	FAD	PZERO	NORMALIZE	DFQ20850
	SLJ	FLOAT		DFQ20860
FLN	SCL	MONE	PUT IN NEGATIVE EXPONENT	DFQ20870
	FAD	PZERO		DFQ20880
	SLJ	FLOAT		DFQ20890
MAXMIN	SLJ	**		DFQ20900
+	THS	=STMAX	TEST FOR MAXIMUM	DFQ20910
	STA	TMAX	A.GT.TMAX	DFQ20920
	STQ	=SSAVQ		DFQ20930
	LDA	SAVQ		DFQ20940
+	THS	=STMIN	TEST FOR MINIMUM	DFQ20950
	SLJ	MAXMIN		DFQ20960
	STA	TMIN	A.LE.TMIN	DFQ20970
	SLJ	MAXMIN		DFQ20980
ALSEV	OCT	-0		DFQ20990
MONE	OCT	2044000000000000		DFQ21000
PZERO	OCT	0		DFQ21010
F1	OCT	2001400000000000		DFQ21020
	END			DFQ21030
	IDENT	SPOPS	SPECIAL OPERATIONS FOR THE	DFQ21040
	CODAP			DFQ21050
OVERFLOW	BLOCK	1		DFQ21060
	COMMON	INDCATOR		DFQ21070
	ORGR	*		DFQ21080
INIT	SLJ	**	INTERVAL PACKAGE. ARGUMENTS ARE	DFQ21090
	STQ	=SX	IN A AND Q. ANSWERS ARE-	DFQ21100
	AJP	3 NEGA	UPPER LIMIT IN A,	DFQ21110
	LDQ	=01	LOWER LIMIT IN Q.	DFQ21120
RET1	STQ	=SSA	STORE SIGN(A)	DFQ21130
	LQC	M12		DFQ21140
	STL	=SMA	MANTISSA(A)	DFQ21150
				DFQ21160

	ARS	36	DFQ21170
	INA	-2000B	DFQ21180
	AJP	*+2	DFQ21190
	AJP	2 *+1	IF NEGATIVE - INCREASE BY 1 DFQ21200
	INA	1	DFQ21210
	STA	=SEA	DFQ21220
	LDA	X	DFQ21230
	AJP	3 NEGX	DFQ21240
	LDQ	=O1	DFQ21250
RET2	STQ	=SSX	STORE SIGN(X) DFQ21260
	LQC	M12	DFQ21270
	STL	=SMX	DFQ21280
	ARS	36	DFQ21290
	INA	-2000B	DFQ21300
	AJP	*+2	DFQ21310
	AJP	2 *+1	IF NEGATIVE - INCREASE BY 1 DFQ21320
	INA	1	DFQ21330
	STA	=SEX	DFQ21340
	SLJ	INIT	--RETURN-- DFQ21350
NEGA	SCM	ALSEV	COMPLEMENT A IF NEGATIVE DFQ21360
	LQC	=O1	-1 TO SIGN(A) DFQ21370
	SLJ	RET1	DFQ21380
NEGX	SCM	ALSEV	COMPLEMENT X IF NEGATIVE DFQ21390
	LQC	=O1	-1 TO SIGN(X) DFQ21400
	SLJ	RET2	DFQ21410
M12	OCT	7777000000000000	DFQ21420
ALSEV	OCT	-0	DFQ21430
N12	OCT	777777777777	DFQ21440
N13	OCT	4000777777777777	DFQ21450
HERD	SLJ	**	-COLLECT BITS AND PIECES- DFQ21460
	STA	=STEMP	SAVE A DFQ21470
+	LDA	EA	DFQ21480
+	AJP	2 *+1	DFQ21490
	SCM	=0777777777777777	DFQ21500
+	THS	=O1777	DFQ21510
+	SLJ	OFLW	DFQ21520
+	LDA	EA	RE-NORMALIZE EXPONENT WRT. 2000 DFQ21530
	AJP	*+2	DFQ21540
	AJP	2 *+1	DFQ21550
	INA	-1	DFQ21560
	INA	2000B	DFQ21570
	ALS	36	DFQ21580
	SCL	N13	DFQ21590
	STA	EA	DFQ21600
	SST	TEMP	FLOAT A DFQ21610
	QJP	NOCARRY	EXEC IF Q=0 DFQ21620

	FAD	=00	NORMALIZE	DFQ21630
	STA	=SSAVA		DFQ21640
	MUI	SA	MULTIPLY BY SIGN	DFQ21650
	STA	=SSAVB		DFQ21660
	LDA	EA		DFQ21670
	INA	1	EXONENT WITH LOW-ORDER 1	DFQ21680
	FAD	SSAVA	ADD TO CHOPPED NUMBER FOR UPPER	DFQ21690
	MUI	SA	MULTIPLY BY SIGN	DFQ21700
	AJP	3 FLIP		DFQ21710
RET3	LDQ	SAVB		DFQ21720
	SLJ	HERD		DFQ21730
FLIP	LRS	48	A TO Q	DFQ21740
	LDA	SAVB	CHOPPED NUMBER TO A	DFQ21750
	SLJ	HERD		DFQ21760
NOCARRY	MUI	SA	EXACT NUMBER TO A	DFQ21770
	FAD	=00		DFQ21780
	STA	SAVB		DFQ21790
	SLJ	RET3		DFQ21800
	ENTRY	SPOPSADD	SP. ADDITION	DFQ21810
SPOPSADD	SLJ	**		DFQ21820
	RTJ	INIT	GO TO INITIALIZE	DFQ21830
	LDA	EA		DFQ21840
	SUB	EX	EA-EX	DFQ21850
	AJP	3 SWITCH	SWITCH IF EX.GT.EA	DFQ21860
RET4	ENQ	0		DFQ21870
+	THS	=0110		DFQ21880
	SLJ	SKIPS		DFQ21890
REASON	SAU	*+1	SHIFT ADDRESS=EA-EX	DFQ21900
	LDA	MX		DFQ21910
	LRS	**	LINE UP MX WITH MA	DFQ21920
RET8	STA	MX		DFQ21930
	LDA	SA	COMPARE SIGNS OF X AND A	DFQ21940
	ADD	SX		DFQ21950
	AJP	SUBTRACT	SUBTRACT IF DIFFERENT SIGNS	DFQ21960
	LDA	MA		DFQ21970
	ADD	MX		DFQ21980
	STA	=STEMP	SAVE SUM	DFQ21990
	SCL	N12	TEST FOR OVERFLOW	DFQ22000
	AJP	NOVER	EXIT FOR NO OVERFLOW	DFQ22010
	LDA	EA		DFQ22020
	INA	1		DFQ22030
	STA	EA		DFQ22040
	LDA	TEMP	AND SHIFT RIGHT BY 1	DFQ22050
	LRS	1		DFQ22060
RET6	RTJ	HERD	GO TO COLLECT	DFQ22070
+	SLJ	SPOPSADD	--EXIT--	DFQ22080

SKIPS	LDA	MX	DFQ22090
	AJP	RET8	DFQ22100
	ENQ	2	DFQ22110
	ENA	0	DFQ22120
	SLJ	RET8	DFQ22130
NOVER	LDA	TEMP	RELOAD ACC DFQ22140
	SLJ	RET6	DFQ22150
SUBTRACT	LDA	MA	SUBTRACT MX FROM MA DFQ22160
	SUB	MX	-NO OVERFLOW POSSIBLE DFQ22170
	AJP	3 NEGATE	IF NEGATIVE - COMPLEMENT, SIGN DFQ22180
	QJP	RET6	NO RESIDUE-EXIT DFQ22190
	INA	-1	NEGATIVE RESIDUE-DECREASE MANTISDFQ22200
	STQ	=SSTORE	DFQ22210
+	AJP	2 *+1	DFQ22220
	ENA	0	DFQ22230
	LQC	STORE	DFQ22240
	SIU	1 GOOUT	DFQ22250
+	ENI	1 83	DFQ22260
	SIU	1 *+1	DFQ22270
+	SCQ	1 **	DFQ22280
	LRS	11	DFQ22290
	STA	TEMP	DFQ22300
	LDA	EA	DFQ22310
	INA	1 -72	DFQ22320
	STA	EA	DFQ22330
GOOUT	ENI	1 **	DFQ22340
	SLJ	NOVER	DFQ22350
NEGATE	LQC	SA	DFQ22360
	STQ	SA	CHANGE SIGN OF RESULT DFQ22370
	SCM	ALSEV	COMPLEMENT ACC DFQ22380
	ENQ	0	NO RESIDUE IN Q POSSIBLE DFQ22390
	SLJ	RET6	DFQ22400
SWITCH	STA	TEMP	INTERCHANGE X AND A DFQ22410
	LDA	EA	DFQ22420
	LDQ	EX	DFQ22430
	STA	EX	DFQ22440
	STQ	EA	DFQ22450
	LDA	MA	DFQ22460
	LDQ	MX	DFQ22470
	STQ	MA	DFQ22480
	STA	MX	DFQ22490
	LDA	SX	DFQ22500
	LDQ	SA	DFQ22510
	STA	SA	DFQ22520
	STQ	SX	DFQ22530
	LAC	TEMP	CHANGE SIGN OF (EA-EX) DFQ22540

	SLJ	RET4		DFQ22550
	ENTRY	SPOPSMUL	SP • MULTIPLICATION	DFQ22560
	SLJ	**		DFQ22570
	RTJ	INIT		DFQ22580
	LDA	EA		DFQ22590
	ADD	EX	ADD EXPONENTS	DFQ22600
	STA	EA	NEW EXPONENT	DFQ22610
	LDA	SA		DFQ22620
	MUI	SX		DFQ22630
	STA	SA	NEW SIGN=SA*SX	DFQ22640
	LDA	MX		DFQ22650
	ALS	11	LEFT-JUSTIFY MULTIPLIER	DFQ22660
	MUF	MA	FORM PRODUCT-NO OVERFLOW POSSIBLE	DFQ22670
	RTJ	ADJUST		DFQ22680
+	RTJ	HERD		DFQ22690
+	SLJ	SPOPSMUL	--EXIT	DFQ22700
	ENTRY	SPOPSDIV	SP • DIVISION	DFQ22710
	SLJ	**		DFQ22720
	RTJ	INIT		DFQ22730
	LDA	EA		DFQ22740
	SUB	EX	NEW EXPONENT=EA-EX+2000	DFQ22750
	INA	1		DFQ22760
	STA	EA		DFQ22770
	LDA	SA	NEW SIGN=SA*SX	DFQ22780
	MUI	SX		DFQ22790
	STA	SA		DFQ22800
	LDA	MX	LEFT-JUSTIFY DIVISOR	DFQ22810
	ALS	11		DFQ22820
	STA	TEMP		DFQ22830
	LDA	MA		DFQ22840
	ENQ	0		DFQ22850
	LRS	1		DFQ22860
	DVF	TEMP	DIVIDE-NO OVERFLOW POSSIBLE	DFQ22870
	RTJ	ADJUST		DFQ22880
+	RTJ	HERD		DFQ22890
+	SLJ	SPOPSDIV		DFQ22900
	OCT	377777777777		DFQ22910
	SLJ	**		DFQ22920
	STA	TEMP		DFQ22930
	SCL	MASKMM		DFQ22940
	AJP	1 ADJUSTA		DFQ22950
	RSO	EA		DFQ22960
	LDA	TEMP		DFQ22970
	LLS	1		DFQ22980
	SLJ	ADJUST		DFQ22990
	ADJUSTA	LDA	TEMP	DFQ23000

	SLJ	ADJUST	DFQ23010
	LDQ	EA	DFQ23020
	QJP	2 OVERI	DFQ23030
	LDA	=04000000000000	DFQ23040
	MUI	SA	DFQ23050
	STA	=SSAVA	DFQ23060
	ENQ	0	DFQ23070
	STQ	=SSAVB	DFQ23080
	AJP	3 FLIP	DFQ23090
	SLJ	HERD	DFQ23100
	ENQ	1	DFQ23110
	STQ	INDCATOR	DFQ23120
	LDA	=0377777777777777	DFQ23130
	MUI	SA	DFQ23140
	STA	=SSAVA	DFQ23150
	STA	=SSAVB	DFQ23160
	LDQ	SAVB	DFQ23170
	SLJ	HERD	DFQ23180
	END		DFQ23190
	FUNCTION LIBINT (ARG)		
	DIMENSION ARG(2),ANS(2)		
	DIMENSION P(6),ARR(2),PIB2(2),TWOPY(2)		
	EQUIVALENCE (PIO2,PIB2),(TWOPY,TWOP1)		
	EQUIVALENCE (LI,SLI),(RI,SRI)		
	EQUIVALENCE (DY,ANS)		
	EQUIVALENCE (PI,P(1)),(PI2,P(3)),(PI3,P(5)),(ARGT,ARR)		
	TYPE INT5(2) D,DY,LIBINT		
	TYPE INT5 (2) ARGT,PIO2,TWOP1		
	TYPE DOUBLE DLOG,DEXP,DCOS,DATAN,DSQRT		
	TYPE DOUBLE PI,PI2,PI3,LI,RI,AL,AR,T1,T2,X		
	DATA(P=2002622077325042B,0550604323046146B,2003622077325042B,		
1	1 0550604323046146B,2004455457437631B,4416443236234514B)		
	DATA(PIB2=2001622077325042B,2001622077325043B),		
	1(TWOPY=2003622077325042B,2003622077325043B)		
	ENTRY LOG5		
	IF(ARG(1))1,1,2		
1	PRINT 19		
19	FORMAT(26H ERROR IN TYPE 5 FUNCTION)		
	RETURN		
2	X=ARG(1)		
	LI=DLOG(X)		
	X=ARG(2)		
	RI=DLOG(X)		
3	CALL ENDPTS (LI,RI,36)		
4	ANS(1)=SLI		
	ANS(2)=SRI		

```

5 LIBINT=DY DFQ23470
RETURN DFQ23480
ENTRY SQRT5 DFQ23490
IF(ARG(1)) 1,1,11 DFQ23500
11 X=ARG(1) DFQ23510
LI=DSQRT(X) DFQ23520
X=ARG(2) DFQ23530
RI=DSQRT(X) DFQ23540
GO TO 3 DFQ23550
ENTRY EXP5 DFQ23560
X=ARG(1) DFQ23570
LI=DEXP(X) DFQ23580
X=ARG(2) DFQ23590
RI=DEXP(X) DFQ23600
CALL ENDPTS (LI,RI,36) DFQ23610
IF(LI)6,4,4 DFQ23620
6 LI=0.0D DFQ23630
GO TO 4 DFQ23640
ENTRY SIN5 DFQ23650
ARR(1)=ARG(1) DFQ23660
ARR(2)=ARG(2) DFQ23670
ARGT=PI02-ARGT DFQ23680
AL=ARR(1) DFQ23690
GO TO 100 DFQ23700
ENTRY COS5 DFQ23710
AL=ARR(1)=ARG(1) DFQ23720
ARR(2)=ARG(2) DFQ23730
100 K=AL/PI2 DFQ23740
IF(AL)101,102,102 DFQ23750
101 K=K-1 DFQ23760
102 ARGT=ARGT-K*TWOP1 DFQ23770
AL=ARR(1) DFQ23780
AR=ARR(2) DFQ23790
T1=AL-PI DFQ23800
IF(T1)110,110,120 DFQ23810
110 T1=AR-PI2 DFQ23820
IF(T1)112,111,111 DFQ23830
111 ANS(1)=-1. DFQ23840
ANS(2)=1. DFQ23850
GO TO 5 DFQ23860
112 T1=AR-PI DFQ23870
IF(T1)113,114,114 DFQ23880
113 LI=DCOS(AR) DFQ23890
RI=DCOS(AL) DFQ23900
GO TO 3 DFQ23910
114 T1=DCOS(AL) DFQ23920

```

T2=DCOS(AR)	DFQ23930
IF(T1-T2)115,115,116	DFQ23940
115 RI=T2	DFQ23950
GO TO 117	DFQ23960
116 RI=T1	DFQ23970
117 CALL ENDPTS (LI,RI,36)	DFQ23980
LI=-1.	DFQ23990
GO TO 4	DFQ24000
120 T1=AR-PI3	DFQ24010
IF(T1)121,111,111	DFQ24020
121 T1=AR-PI2	DFQ24030
IF(T1)122,123,123	DFQ24040
122 LI=DCOS(AL)	DFQ24050
RI=DCOS(AR)	DFQ24060
GO TO 3	DFQ24070
123 T1=DCOS(AL)	DFQ24080
T2=DCOS(AR)	DFQ24090
IF(T1-T2)124,124,125	DFQ24100
124 LI=T1	DFQ24110
GO TO 126	DFQ24120
125 LI=T2	DFQ24130
126 CALL ENDPTS (LI,RI,36)	DFQ24140
RI=1.	DFQ24150
GO TO 4	DFQ24160
ENTRY ATAN5	DFQ24170
X=ARG(1)	DFQ24180
LI=DATAN(X)	DFQ24190
X=ARG(2)	DFQ24200
RI=DATAN(X)	DFQ24210
GO TO 3	DFQ24220
ENTRY ABS5	DFQ24230
IF(ARG(1))13,15,15	DFQ24240
13 IF(ARG(2)) 14,14,16	DFQ24250
16 ANS(1)=0.	DFQ24260
IF(ARG(2)+ARG(1))17,18,18	DFQ24270
17 ANS(2)=-ARG(1)	DFQ24280
GO TO 5	DFQ24290
18 ANS(2)=ARG(2)	DFQ24300
GO TO 5	DFQ24310
14 ANS(2)=-ARG(1)	DFQ24320
ANS(1)=-ARG(2)	DFQ24330
GO TO 5	DFQ24340
15 ANS(1)=ARG(1)	DFQ24350
ANS(2)=ARG(2)	DFQ24360
GO TO 5	DFQ24370
ENTRY CDFN5	DFQ24380

```

Y=ARG(1) DFQ24390
LI=CDFN(Y) DFQ24400
Y=ARG(2) DFQ24410
RI=CDFN(Y) DFQ24420
CALL ENDPTS (LI,RI,27) DFQ24430
GO TO 4 DFQ24440
END DFQ24450
SUBROUTINE ENDPTS(LEP,REP,NOBITS) DFQ24460
TYPE REAL LEP DFQ24470
IADJ=2** (36-NOBITS) DFQ24480
EP=2.**(-NOBITS) DFQ24490
ITEMP=IADJ-1 DFQ24500
IMASK=.NOT.ITEMP DFQ24510
ZEP=ABSF(LEP) DFQ24520
ASSIGN 20 TO IEND DFQ24530
IF (LEP)200,100,100 DFQ24540
20 IF(LEP)21,22,22 DFQ24550
21 ANS=-ANS DFQ24560
22 LEP=ANS DFQ24570
ZEP=ABSF(REP) DFQ24580
ASSIGN 30 TO IEND DFQ24590
IF(REP)100,200,200 DFQ24600
30 IF(REP)31,32,32 DFQ24610
31 ANS=-ANS DFQ24620
32 REP=ANS DFQ24630
RETURN DFQ24640
100 TEMP1=(ZEP.AND.7777000000000000B).OR.IADJ DFQ24650
TEMP2=(ZEP.AND.IMASK) DFQ24660
ANS=TEMP2-TEMP1 DFQ24670
IF(ABSF(ANS).LT.EP)101,102 DFQ24680
101 ANS=-EP DFQ24690
102 GO TO IEND DFQ24700
200 TEMP1=(ZEP.AND.7777000000000000B).OR.IADJ DFQ24710
TEMP2=ZEP.AND.IMASK DFQ24720
ANS=TEMP2+TEMP1+TEMP1 DFQ24730
IF(ABSF(ANS).LT.EP)201,202 DFQ24740
201 ANS=EP DFQ24750
202 GO TO IEND DFQ24760
END DFQ24770
SUBROUTINE ERRORINT DFQ24780
COMMON/OVERFLOW/INDCATOR DFQ24790
INDCATOR=1 DFQ24800
RETURN DFQ24810
END DFQ24820

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